Sampling
Why Sample?

• Why not study everyone?
• Debate about Census vs. sampling
Problems in Sampling?

• What problems do you know about?
• What issues are you aware of?
• What questions do you have?
Key Sampling Concepts

Who do you want to generalize to?

The Theoretical Population

What population can you get access to?

The Study Population

How can you get access to them?

The Sampling Frame

Who is in your study?

The Sample

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Sampling Process

Units of Analysis (people)

- **Target Population**
  - Population of Interest

- **Actual Population to Which Generalizations Are Made**
  - Defined/Listed by Sampling Frame

- **Target Sample**
  - The people actually studied

List or Procedure

- **Sampling Frame**
  - List or Rule Defining the Population

- **List of Target Sample**
  - Method of selection

**Generalization**

**Response Rate**
Key Ideas

• Distinction between the population of interest and the actual population defined by the sampling frame
• Generalizations can be made only to the actual population
• Understand crucial role of the sampling frame
Sampling Frame

- The list or procedure defining the POPULATION. (From which the sample will be drawn.)
- Distinguish sampling frame from sample.
- Examples:
  - Telephone book
  - Voter list
  - Random digit dialing
- Essential for probability sampling, but can be defined for nonprobability sampling
Types of Samples

- Probability
  - Simple Random
  - Systematic Random
  - Stratified Random
  - Random Cluster
  - Stratified Cluster
  - Complex Multi-stage Random (various kinds)

- Non-Probability
  - Quota
  - Convenience
  - Purposive
Probability Samples

• A probability sample is one in which each element of the population has a **known non-zero** probability of selection.

• Not a probability sample of some elements of population cannot be selected (have zero probability)

• Not a probability sample if probabilities of selection are not known.
Probability Sampling

- Cannot guarantee "representativeness" on all traits of interest
- A sampling plan with known statistical properties
- Permits statements like: "The probability is .99 that the true population correlation falls between .46 and .56."
Sampling Frame is Crucial in Probability Sampling

• If the sampling frame is a poor fit to the population of interest, random sampling from that frame cannot fix the problem
• The sampling frame is non-randomly chosen. Elements not in the sampling frame have zero probability of selection.
• Generalizations can be made ONLY to the actual population defined by the sampling frame
Types of Probability Samples

- Simple Random
- Systematic Random
- Stratified Random
- Random Cluster
- Stratified Cluster
- Complex Multi-stage Random (various kinds)
Simple Random Sampling

• Each element in the population has an equal probability of selection AND each combination of elements has an equal probability of selection
• Names drawn out of a hat
• Random numbers to select elements from an ordered list
Stratified Random Sampling

- Divide population into groups that differ in important ways
- Basis for grouping must be known before sampling
- Select random sample from within each group
Stratified Random Sampling-2

• For a given sample size, reduces error compared to simple random sampling IF the groups are different from each other
• Tradeoff between the cost of doing the stratification and smaller sample size needed for same error
• Probabilities of selection may be different for different groups, as long as they are known
• Oversampling small groups improves inter-group comparisons
Systematic Random Sampling-1

- Each element has an equal probability of selection, but combinations of elements have different probabilities.
- Population size $N$, desired sample size $n$, sampling interval $k=N/n$.
- Randomly select a number $j$ between 1 and $k$, sample element $j$ and then every $k^{th}$ element thereafter, $j+k$, $j+2k$, etc.
- Example: $N=64$, $n=8$, $k=64/8=8$. Random $j=3$. 
Systematic Random Sampling-2

- Has same error rate as simple random sample if the list is in random or haphazard order
- Provides the benefits of implicit stratification if the list is grouped
Systematic Random Sampling-3

- Runs the risk of error if periodicity in the list matches the sampling interval
- This is rare.
- In this example, every 4\textsuperscript{th} element is red, and red never gets sampled. If j had been 4 or 8, ONLY reds would be sampled.
Random Cluster Sampling - 1

- Done correctly, this is a form of random sampling
- Population is divided into groups, usually geographic or organizational
- Some of the groups are randomly chosen
- In pure cluster sampling, whole cluster is sampled.
- In simple multistage cluster, there is random sampling within each randomly chosen cluster
Random Cluster Sampling - 2

- Population is divided into groups
- Some of the groups are randomly selected
- For given sample size, a cluster sample has more error than a simple random sample
- Cost savings of clustering may permit larger sample
- Error is smaller if the clusters are similar to each other
Random Cluster Sampling - 3

- Cluster sampling has very high error if the clusters are different from each other
- Cluster sampling is NOT desirable if the clusters are different
- It IS random sampling: you randomly choose the clusters
- But you will tend to omit some kinds of subjects
Stratified Cluster Sampling

- Reduce the error in cluster sampling by creating strata of clusters
- Sample one cluster from each stratum
- The cost-savings of clustering with the error reduction of stratification
## Stratification vs. Clustering

<table>
<thead>
<tr>
<th>Stratification</th>
<th>Clustering</th>
</tr>
</thead>
<tbody>
<tr>
<td>• Divide population into groups different from each other: sexes, races, ages</td>
<td>• Divide population into comparable groups: schools, cities</td>
</tr>
<tr>
<td>• Sample randomly from each group</td>
<td>• Randomly sample some of the groups</td>
</tr>
<tr>
<td>• Less error compared to simple random</td>
<td>• More error compared to simple random</td>
</tr>
<tr>
<td>• More expensive to obtain stratification information before sampling</td>
<td>• Reduces costs to sample only some areas or organizations</td>
</tr>
</tbody>
</table>
Stratified Cluster Sampling

- Combines elements of stratification and clustering
- First you define the clusters
- Then you group the clusters into strata of clusters, putting similar clusters together in a stratum
- Then you randomly pick one (or more) cluster from each of the strata of clusters
- Then you sample the subjects within the sampled clusters (either all the subjects, or a simple random sample of them)
Multi-stage Probability Samples –1

- Large national probability samples involve several stages of stratified cluster sampling
- The whole country is divided into geographic clusters, metropolitan and rural
- Some large metropolitan areas are selected with certainty (certainty is a non-zero probability!)
- Other areas are formed into strata of areas (e.g. middle-sized cities, rural counties); clusters are selected randomly from these strata
Multi-stage Probability Samples –2

- Within each sampled area, the clusters are defined, and the process is repeated, perhaps several times, until blocks or telephone exchanges are selected.
- At the last step, households and individuals within household are randomly selected.
- Random samples make multiple call-backs to people not at home.
The Problem of Non-Response - 1

• You can randomly pick elements from sampling frame and use them to randomly select people
• But you cannot make people respond
• Non-response destroys the generalizeability of the sample. You are generalizing to people who are willing to respond to surveys
• If response is 90% or so, not so bad. But if it is 50%, this is a serious problem
Multiple call-backs are essential for trying to reduce non-response bias.

Samples without call-backs have high bias: cannot really be considered random samples.

Response rates have been falling.

It is very difficult to get above a 60% response rate.

You do the best you can, and try to estimate the effect of the error by getting as much information as possible about the predictors of non-response.
Non-probability Samples

- Convenience
- Purposive
- Quota
Convenience Sample

- Subjects selected because it is easy to access them.
- No reason tied to purposes of research.
- Students in your class, people on State Street, friends
Purposive Samples

- Subjects selected for a good reason tied to purposes of research
- Small samples < 30, not large enough for power of probability sampling.
  - Nature of research requires small sample
  - Choose subjects with appropriate variability in what you are studying
- Hard-to-get populations that cannot be found through screening general population
Quota Sampling

- Pre-plan number of subjects in specified categories (e.g. 100 men, 100 women)
- In uncontrolled quota sampling, the subjects chosen for those categories are a convenience sample, selected any way the interviewer chooses
- In controlled quota sampling, restrictions are imposed to limit interviewer’s choice
- No call-backs or other features to eliminate convenience factors in sample selection
Quota Vs Stratified Sampling

- In Stratified Sampling, selection of subject is random. Call-backs are used to get that particular subject.
- Stratified sampling without call-backs may not, in practice, be much different from quota sampling.

- In Quota Sampling, interviewer selects first available subject who meets criteria: is a *convenience sample*.
- Highly controlled quota sampling uses probability sampling down to the last block or telephone exchange.

But you should know the difference for the test!!
Sample Size

- Heterogeneity: need larger sample to study more diverse population
- Desired precision: need larger sample to get smaller error
- Sampling design: smaller if stratified, larger if cluster
- Nature of analysis: complex multivariate statistics need larger samples
- Accuracy of sample depends upon sample size, not ratio of sample to population
Sampling in Practice

- Often a non-random selection of basic sampling frame (city, organization etc.)
- Fit between sampling frame and research goals must be evaluated
- Sampling frame as a concept is relevant to all kinds of research (including nonprobability)
- Nonprobability sampling means you cannot generalize beyond the sample
- Probability sampling means you can generalize to the population defined by the sampling frame