and marginal costs are

$$
\begin{aligned}
M C(y) & =1 \\
M C(y) & =\frac{1}{2} \frac{1}{\sqrt{y}} \\
M C(y) & =2 y
\end{aligned}
$$



## Problem 4 (Cost curves)

a) Decreasing - the exponent in the cost function is greater than one.
b) Total cost function is
hence $T C(1)=8, T C(2)=20$ and $T C(4)=68$.

c) The average fixed cost as a function of $y$ is given by

$$
A F C(y)=\frac{4}{y}
$$

and hence $A F C(1)=4, A F C(2)=2$ and $A F C(4)=1$. It becomes zero as $y$ gets larger (with large production the constant fixed cost per unit becomes negligible) and it goes to infinity as $y$ approaches zero.

d) The average cost function is linear and is given by

$$
A V C(y)=4 y
$$

and hence $A V C(1)=4, A V C(2)=8$ and $A V C(4)=16$
e) Average total cost is given by

$$
A T C=A V C+A F C=4 y+\frac{4}{y}
$$

