

10-6-09

"OPTIMAL" SUBSIDY/TAX?

NOW: PRICE COMPETITION  
(DIFF. PRODUCT)

MODEL 1:

— COUNTRY 1 GOVERNMENT  
— CHOOSES SUBS/TAX  
TO EXPORTS

— FIRMS COMPETE  
CHOOSING PRICES  
SIMULTANEOUSLY

RESULT: "OPTIMAL POLICY IS A TAX!"

$w_1, w_2$  HIGHER THAN  
WITHOUT INTERVENTION

MODEL 2:

— BOTH COUNTRIES CHOOSE  
SUBS/TAX TO EXPORTS

— FIRMS COMPETE CHOOSING  
PRICES SIMULTANEOUSLY

RESULT: BOTH COUNTRIES CHOOSE  
TO TAX  $w_1, w_2$  HIGHER THAN  
IN MODEL 1

# MODEL 1

(2)

$$q_1 = 168 - 2p_1 + p_2$$

$$q_2 = 168 - 2p_2 + p_1$$

$$MC_1 = MC_2 = 0$$

NOTATION:

$$C_1 = MC_1 - S_1$$

$$C_2 = MC_2 - S_2$$

STEP 1: NE in prices as functions of  $C_1, C_2$

$$\begin{aligned} \text{MAX}_{p_1} \pi_1(\cdot) &= p_1 q_1 - C_1 q_1 \\ &= [p_1 - C_1] q_1 \\ &= [p_1 - C_1] [168 - 2p_1 + p_2] \end{aligned}$$

$$\frac{\partial}{\partial p_1} = 0 \implies p_1 = R_1(p_2) \quad (*)$$

SIMILARLY

$$\text{MAX}_{p_2} \pi_2(\cdot) = [p_2 - C_2] [168 - 2p_2 + p_1]$$

$$\frac{\partial}{\partial p_2} = 0 \implies p_2 = R_2(p_1) \quad (**)$$

Solving  $(*)$ ,  $(**)$

NE PRICES:

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$$p_1 = 56 + \frac{8}{15} C_1 + \frac{2}{15} C_2$$

$$p_2 = 56 + \frac{8}{15} C_2 + \frac{2}{15} C_1$$

STEP 1:

MAX  
 $s_1$

$$\begin{aligned} W_1 &= [p_1 - \underset{\substack{\downarrow \\ MC_1 - s_1}}{C_1}] q_1 - s_1 q_1 \\ &= [p_1 - MC_1 + s_1] q_1 - s_1 q_1 \\ &= [p_1 - \underset{\substack{= \\ 0}}{MC_1}] q_1 = p_1^{NE} q_1^{NE} \end{aligned}$$

IN THIS CASE ( $s_1 > 0, s_2 = 0$ )  
THE NE PRICES / QUANT. ARE

$$\boxed{p_1^{NE}} = 56 + \frac{8}{15} (-s_1)$$

$$\boxed{p_2^{NE}} = 56 + \frac{2}{15} (-s_1)$$

$$\begin{aligned} \boxed{q_1^{NE}} &= 168 - 2p_1 + p_2 \\ &= \boxed{112 + \frac{14}{15} s_1} \end{aligned}$$

MAX\_{S\_1} W\_1 = p\_1 q\_1

= [56 - \frac{8}{15} S\_1] [112 + \frac{14}{15} S\_1]

\frac{dW\_1}{dS\_1} = -\frac{8}{15} [112 + \frac{14}{15} S\_1] +

\frac{14}{15} [56 - \frac{8}{15} S\_1] = 0

\Rightarrow S\_1^\* = -7.5 TAX!

\Rightarrow C\_1 = 7.5  
C\_2 = 0

p\_1^{NE} = 60 p\_2 = 57

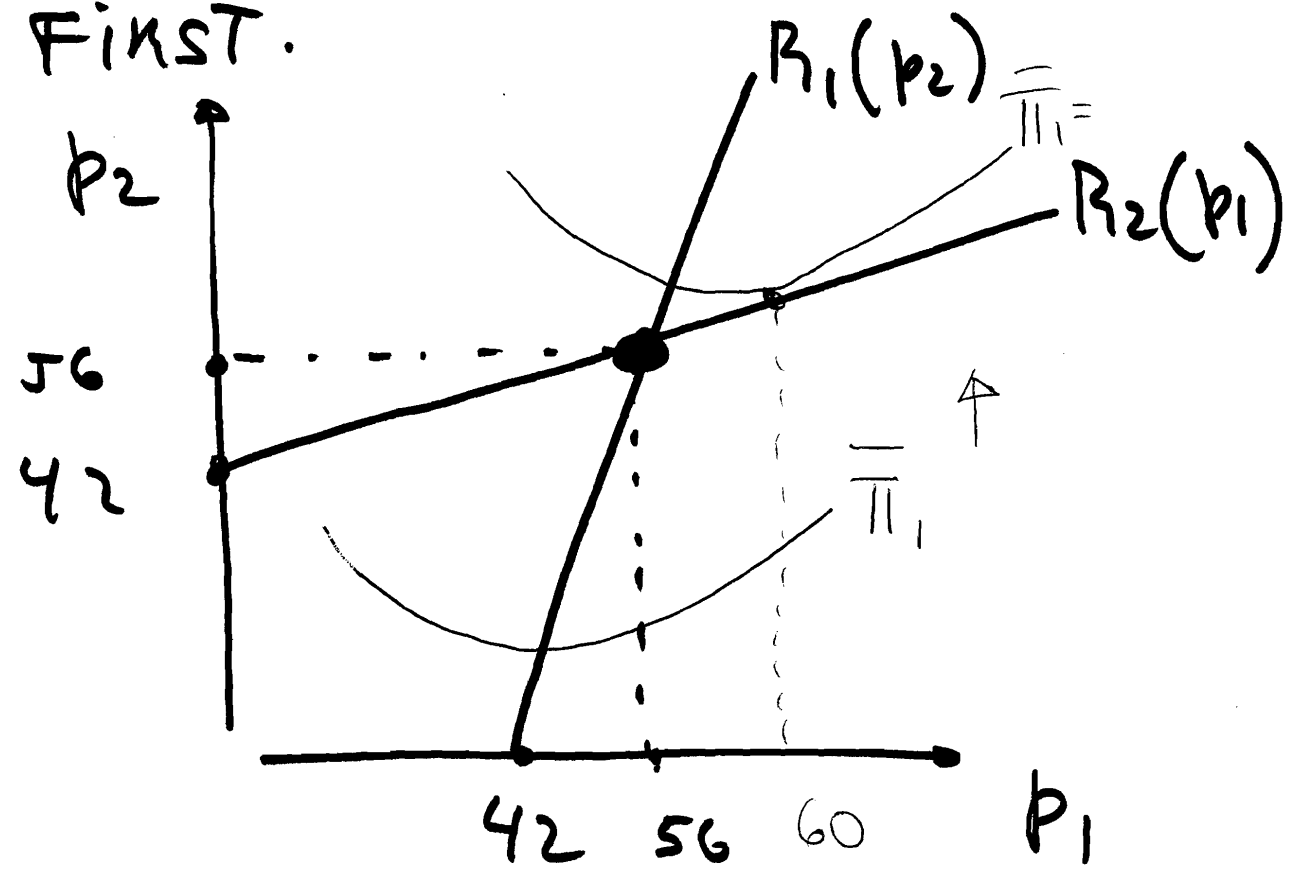
W\_1 = \pi\_1 = 6300 W\_2 = \pi\_2 = 6498

PROD. PROFITS

REMARKS: 1) PROFITS HIGHER THAN WHEN THERE IS NO GOV. INTERVENTION: p\_1 = p\_2 = 56 \pi\_1 = \pi\_2 = 6272

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② OUTCOME COINCIDES WITH OUTCOME OF THE SEQ. PRICE GAME (NO GOV. INTERVENTION) WHEN FIRM 1 CHOOSES PRICE FIRST.



MODEL 2 :

- BOTH GOV. CHOOSE  $s_1, s_2 \geq 0$
- FIRMS COMPETE IN PRICES

STEP 1 : CALCULATE NE IN PRICES ASSUMING FIRMS HAVE  $c_1, c_2$  AS EFF. MARGINAL COSTS

NE IN  $s_1, s_2$  { STEP 2 : GOV. MAX WELFARE & CHOOSE  $s_1, s_2$  SIMULTANEOUSLY

STEP 1 : SEE EF. IN PAGE 3

STEP 2 : FIND NE IN  $s_1, s_2$

$$\begin{aligned} \text{MAX}_{s_1} w_1 &\implies \frac{\partial}{\partial s_1} = 0 \\ \text{MAX}_{s_2} w_2 &\implies \frac{\partial}{\partial s_2} = 0 \implies \end{aligned}$$

RESULT:

$$s_1 = s_2 = -7.6$$

$$p_1 = p_2 = 61.07$$

$$q_1 = q_2 = 106.9$$

$$w_1 = w_2 = (p_1 - mc_1) q_1 = (p_2 - mc_2) q_2 = 6,528$$

REMARK:

TO MAXIMIZE  $w_1$ , WE TAKE  $s_2$  AS A CONSTANT.

$$w_1 = p_1 \cdot q_1 =$$

WHERE

$$p_1 = 56 + \frac{8}{15} [-s_1] + \frac{2}{15} [-s_2]$$

$$q_1 = 168 - 2p_1 + p_2$$

Given next

$$p_2 = 56 + \frac{8}{15} (-s_2) + \frac{2}{15} (-s_1) \quad \textcircled{8}$$

$$w_1 = \left\{ 56 + \frac{8}{15} [-s_1] + \frac{2}{15} [-s_2] \right\}$$
$$\left\{ 168 - 2 \underbrace{[\quad]}_{p_1} + \underbrace{[\quad]}_{p_2} \right\}$$