

Econ 702 Macroeconomics I

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Spring 2020

Lecture 26: Financial Frictions

## Outline

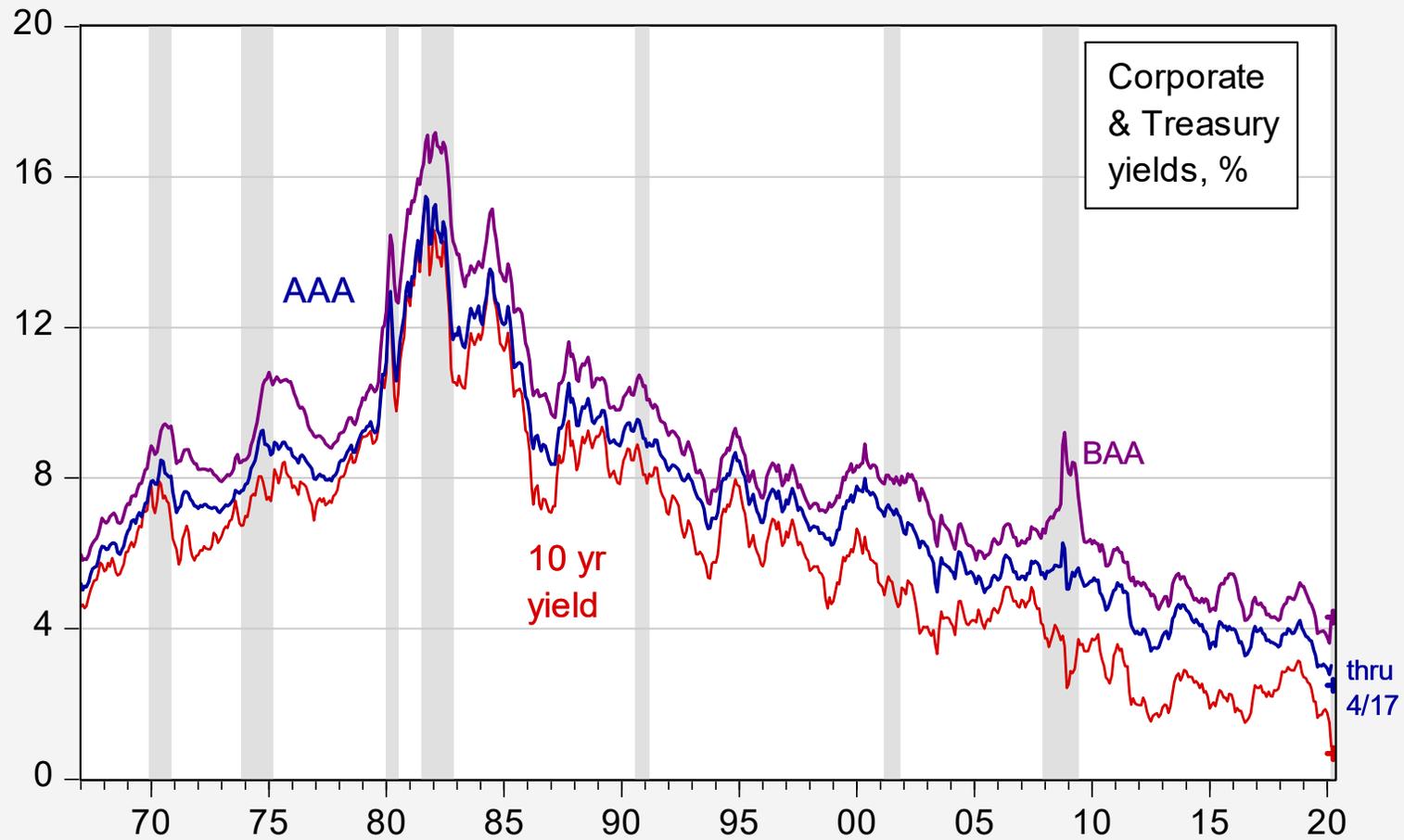
- Overview
- Frictions the when Spread is Exogenous
- Exogenous Spread & Financial Crises/Recessions
- The Endogenous Component of Spread

# Overview

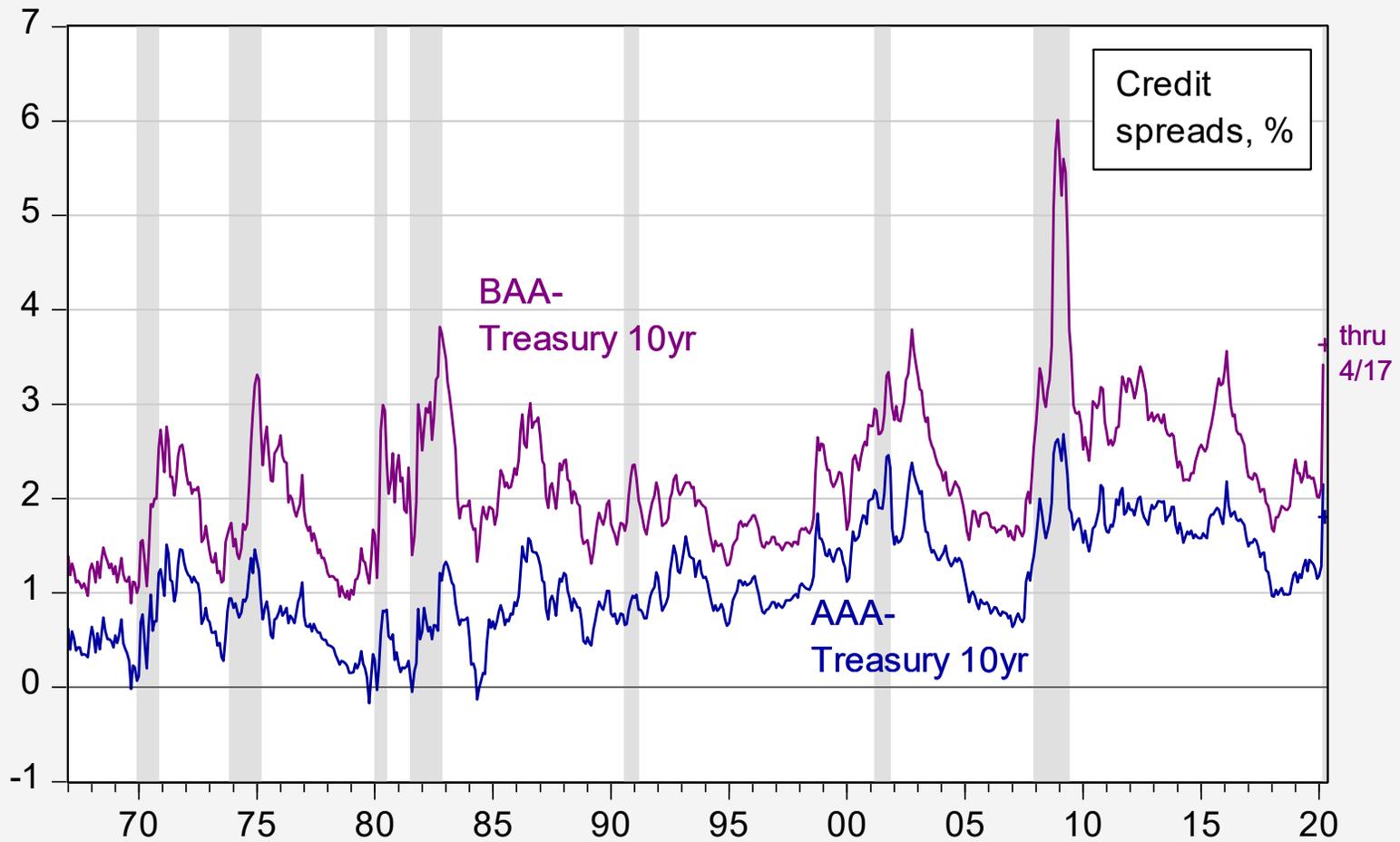
# Overview: Financial Frictions

- So far in all the treatments, risk and uncertainty do not make an explicit appearance
- Financial problems do not make an appearance at all (at least not in the second half of the course)
- Marginal product of capital equals real interest rate
- Households, firms can borrow as much as they want at the given interest rate
- There is no quantity rationing
- But we know some firms pay more to borrow than others – and the excess of borrowing rates over a risk free rate varies over time
- Suggests using the credit spread

# Corporate Bond Yields



# Credit Spreads



Note: Corp bond yields pertain to mixed and changing average maturities

Where's the spread,  $f$ , show up?

$$C_t = C^d(Y_t - G_t, Y_{t+1} - G_{t+1}, r_t) \quad (35.1)$$

$$N_t = N^s(w_t, \theta_t) \quad (35.2)$$

$$P_t = \bar{P}_t + \gamma(Y_t - Y_t^f) \quad (35.3)$$


$$I_t = I^d(r_t + f_t, A_{t+1}, K_t) \quad (35.4)$$

$$Y_t = A_t F(K_t, N_t) \quad (35.5)$$

$$Y_t = C_t + I_t + G_t \quad (35.6)$$

$$M_t = P_t M^d(r_t + \pi_{t+1}^e, Y_t) \quad (35.7)$$

$$r_t = i_t - \pi_{t+1}^e \quad (35.8)$$

# Frictions when Spread Is Exogenous

# Banks, Government

Intermediary takes deposits,  $S$ , makes loans  $B^I$  and  $B^G$  to firms and govt,  $D^I$  is firm dividends

$$D_{t+1}^I = (r_t + f_t)B_t^I + r_t B_t^G - r_t S_t \quad (35.9)$$

Govt borrows and taxes to spend s.t. intertemporal budget constraint

$$G_t \leq T_t + B_t^G \quad (35.10)$$

$$G_t + r_t B_t^G \leq T_{t+1} + B_{t+1}^G - B_t^G \quad (35.11)$$

# Households

Unchanged relative to previous. Optimize

$$C_t + S_t \leq w_t N_t + D_t - T_t \quad (35.12)$$

$$C_{t+1} + S_{t+1} \leq w_{t+1} N_{t+1} - T_{t+1} + D_{t+1} + D_{t+1}^I + (1 + r_t) S_t \quad (35.13)$$

$$U = u(C_t, 1 - N_t) + \beta u(C_{t+1}, 1 - N_{t+1}) \quad (35.14)$$

## FOCs

$$u_C(C_t, 1 - N_t) = \beta(1 + r_t) u_C(C_{t+1}, 1 - N_{t+1}) \quad (35.15)$$

$$u_L(C_t, 1 - N_t) = w_t u_C(C_t, 1 - N_t) \quad (35.16)$$

$$u_L(C_{t+1}, 1 - N_{t+1}) = w_{t+1} u_C(C_{t+1}, 1 - N_{t+1}) \quad (35.17)$$

# Firms

Maximize  $V$  by choosing  $N$ , or  $I$

$$\begin{aligned}
 \max_{N_t, I_t} \quad & V_t = A_t F(K_t, N_t) - w_t N_t + \\
 & \frac{1}{1+r_t} \left[ \underbrace{A_{t+1} F(K_{t+1}, N_{t+1}) + (1-\delta)K_{t+1}}_{\text{Liquidation Value}} - w_{t+1} N_{t+1} - \underbrace{(1+r_t+f_t)B_t^I}_{\text{Financing Cost}} \right] \quad (35.18)
 \end{aligned}$$

$D_t + \frac{D_{t+1}}{1+r_t}$

Where investment follows law of motion:

$$K_{t+1} = I_t + (1 - \delta)K_t$$

Recast problem as Max  $K_{t+1}$

Since

$$B_t^I = I_t = K_{t+1} - (1 - \delta)K_t$$

$$\max_{N_t, K_{t+1}} V_t = A_t F(K_t, N_t) - w_t N_t + \frac{1}{1 + r_t} \left[ A_{t+1} F(K_{t+1}, N_{t+1}) + (1 - \delta)K_{t+1} - w_{t+1} N_{t+1} - (1 + r_t + f_t)(K_{t+1} - (1 - \delta)K_t) \right] \quad (35.19)$$

Then FOCs are:

$$\frac{\partial V_t}{\partial N_t} = 0 \Leftrightarrow A_t F_N(K_t, N_t) = w_t \quad (35.20)$$

$$\frac{\partial V_t}{\partial K_{t+1}} = 0 \Leftrightarrow r_t + f_t + \delta = A_{t+1} F_K(K_{t+1}, N_{t+1}) \quad (35.21)$$

# When Will Equilibrium Be Same as Social Planner's Solution?

$$u_C(C_t, 1 - N_t) = \beta u_C(C_{t+1}, 1 - N_{t+1})(A_{t+1}F_K(K_{t+1}, N_{t+1} + (1 - \delta))) \quad (35.22)$$

Combining (35.21) with (35.15), we would obtain:

$$u_C(C_t, 1 - N_t) = \beta u_C(C_{t+1}, 1 - N_{t+1})(A_{t+1}F_K(K_{t+1}, N_{t+1} + (1 - \delta) - f_t)) \quad (35.23)$$

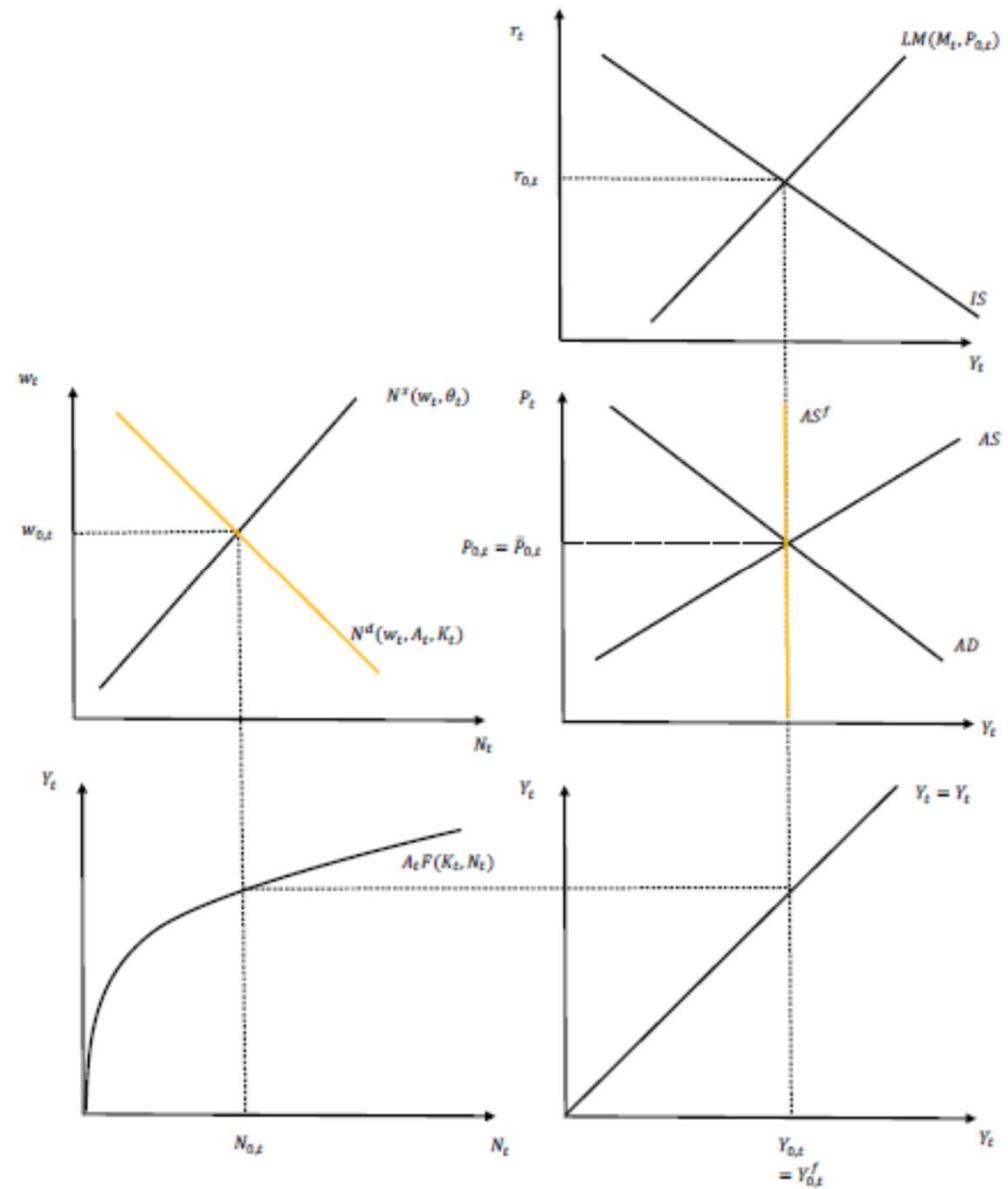
$f > 0$  implies consumption too high, investment too low, relative to social planner's solution

# The Exogenous Spread and Financial Crises/Recessions

# Equilibrium

Hard to see any impact of  $f$  in medium run equilibrium; one needs to have a shock

Figure 35.2: Equilibrium in the Partial Sticky Price Model with Financial Frictions



Where's the spread,  $f$ , show up?

$$C_t = C^d(Y_t - G_t, Y_{t+1} - G_{t+1}, r_t) \quad (35.1)$$

$$N_t = N^s(w_t, \theta_t) \quad (35.2)$$

$$P_t = \bar{P}_t + \gamma(Y_t - Y_t^f) \quad (35.3)$$


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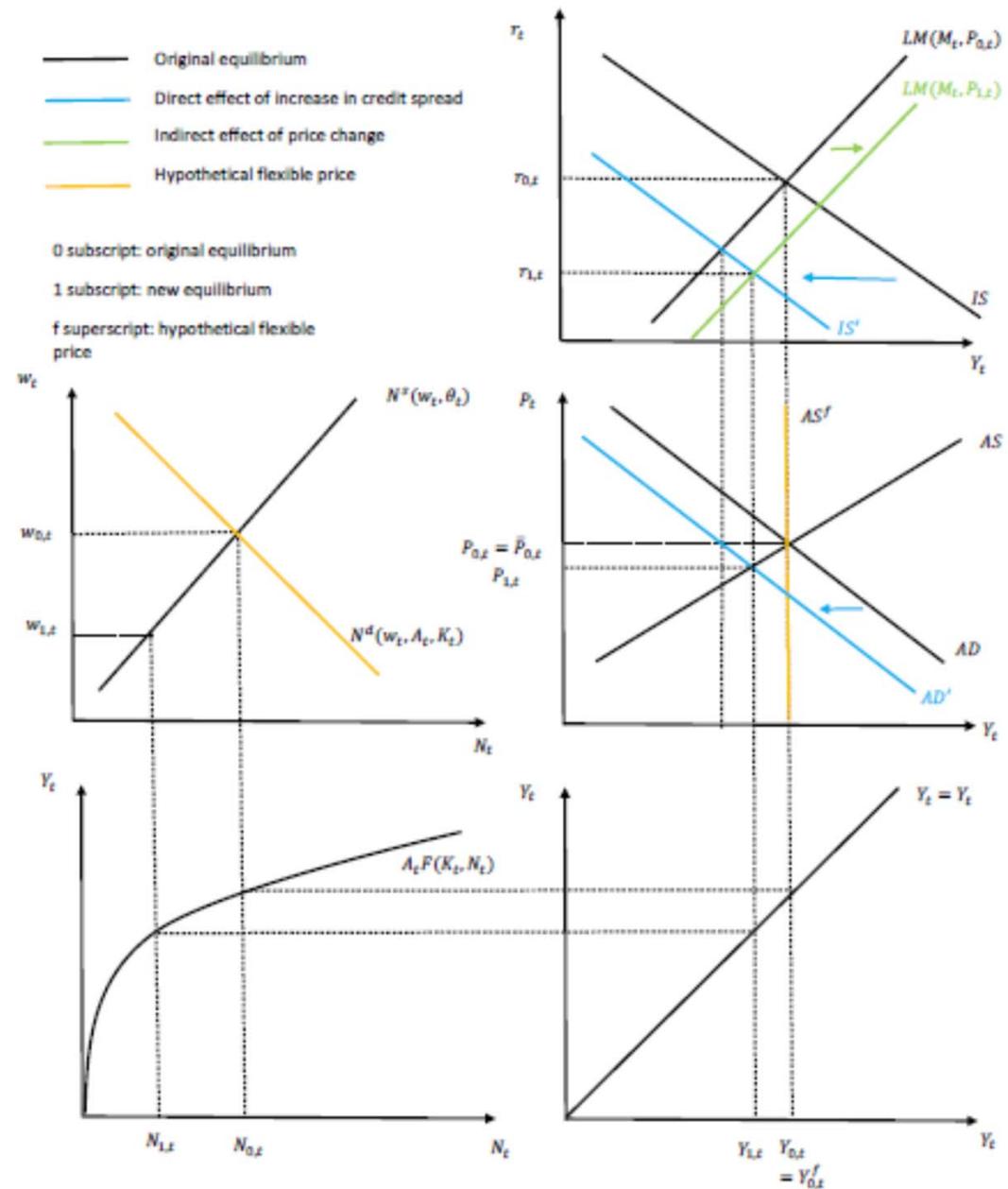
$$M_t = P_t M^d(r_t + \pi_{t+1}^e, Y_t) \quad (35.7)$$

$$r_t = i_t - \pi_{t+1}^e \quad (35.8)$$

Figure 35.3: Increase in Credit Spread

Exogenous increase in  $f$

- IS shifts in (blue arrow)
- P falls (move along AS)
- LM shifts out (green arrow)
- Output falls
- $r$  is lower, but w/higher  $f$ ,  $l$  lower

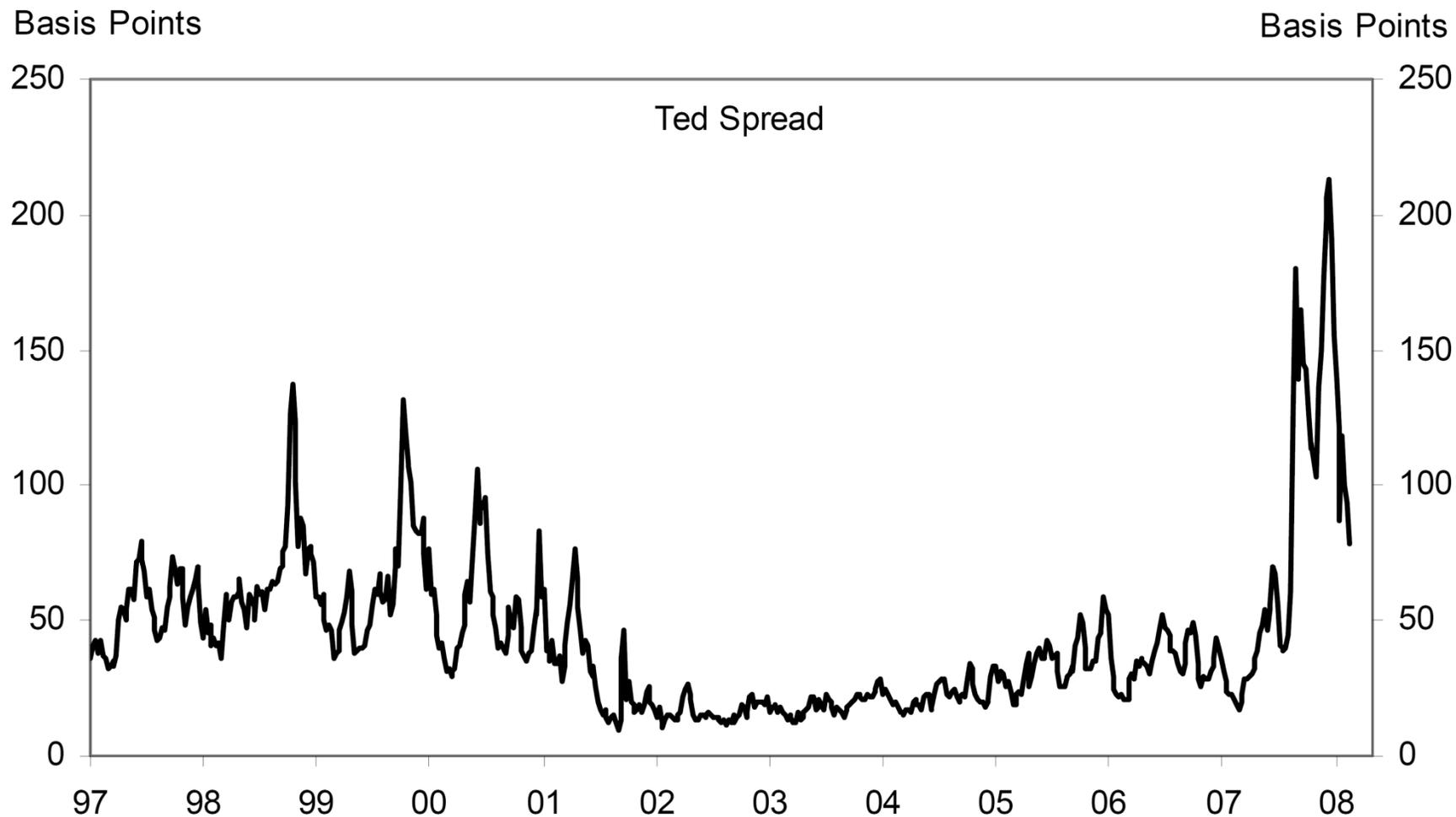


# Interpreting Exogenous Increases in $f$

- Exogenous increases associated with “runs” on banks, panics
- Example is 2007-08 financial crisis where suddenly lots of bank assets were perceived as lower value than previously
- Here  $f$  moves in a way exogenous with respect to the business cycle
- But other movements in  $f$  a way endogenous with respect to the business cycle

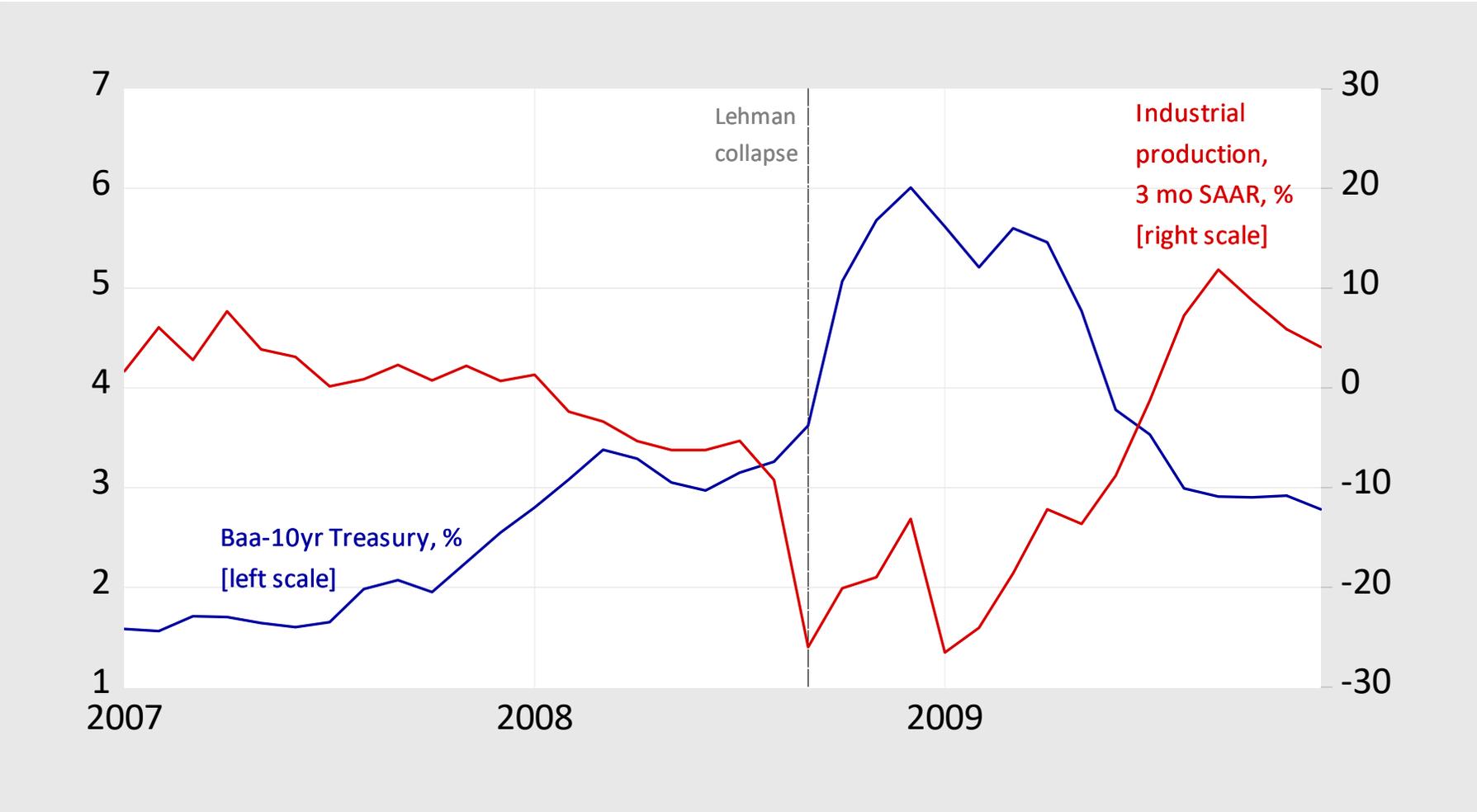
# One Proxy – 3 month Libor-US Treasury

Exhibit 2.8 Treasury-Eurodollar (TED) Spread



Source: Financial Times. Federal Reserve Board.

# Credit Spread during Great Financial Crisis



# The Endogenous Component of the Spread

## Interpreting Endogenous Changes in $f$

- But other movements in  $f$  a way endogenous with respect to the business cycle
- This feedback between business cycle and credit spread can be called a financial accelerator model
- Arises because of collateral constraints limit how much can be borrowed (Bernanke, Gertler & Gilchrist, 1999)
- Summarize as:

$$f_t = \bar{f}_t - aY_t \quad (35.24)$$

# Intuition for Financial Accelerator

- Firms can only invest out of borrowing
- But firms can only borrow as much as value of capital stock (minus debt), which can be seized (this is called a collateral constraint)
- Value of capital stock goes down
  - during economic downturns as sales go down
  - as real interest rates go up

# Collateral Constraints: Recession induced decline in capital value

Pre-Shock Firm Balance Sheet	
Assets	Liabilities
Capital (1 million machines × \$1000/machine = \$1 billion)	Debt (\$700 million)
	Equity (\$300 million)

Net worth = \$300 million

Post-Shock Firm Balance Sheet	
Assets	Liabilities
Capital (1 million machines × \$800/machine = \$1 billion)	Debt (\$700 million)
	Equity (\$100 million)

Price of machines falls by 20%  
Net worth = \$100 million

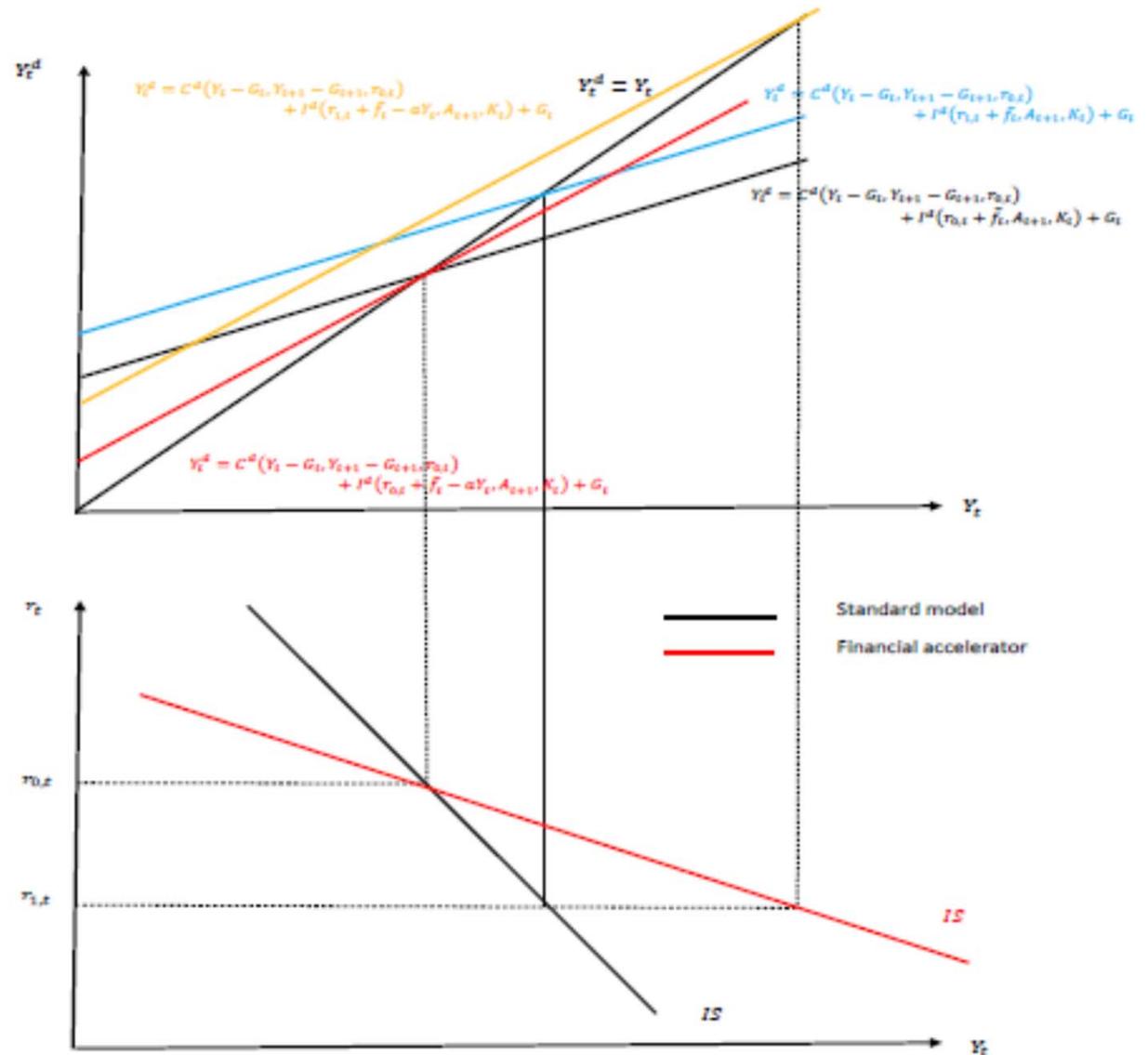
# Intuition for Financial Accelerator

- But if all firms behave the same, investment falls reducing aggregate demand, which further reduces value of capital, hence borrowing, hence investment
- Cycle repeats...
- This implies any change in  $r$  results in larger change in AD
- I.e., flatter IS curve

# Derivation of IS

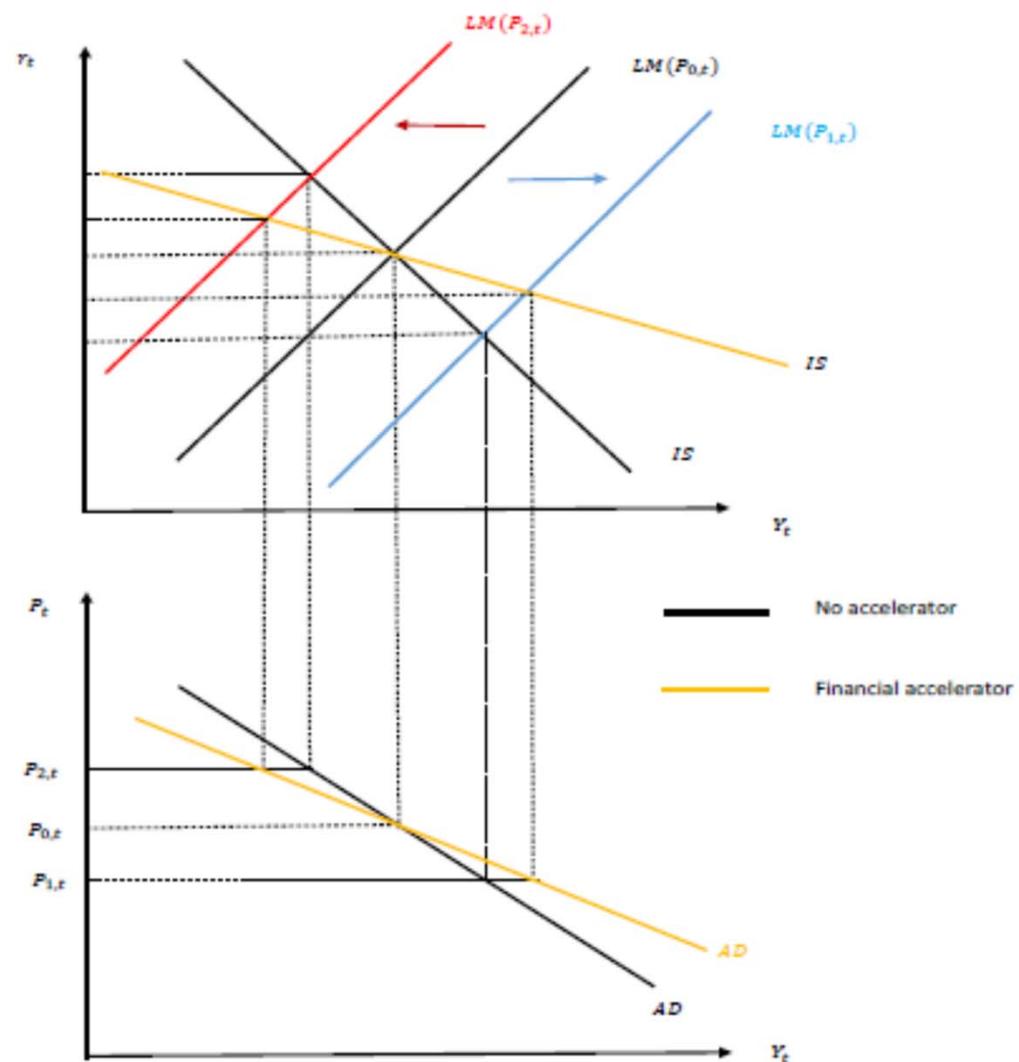
- Feedback leads to flatter IS

Figure 35.4: The IS Curve with the Financial Accelerator



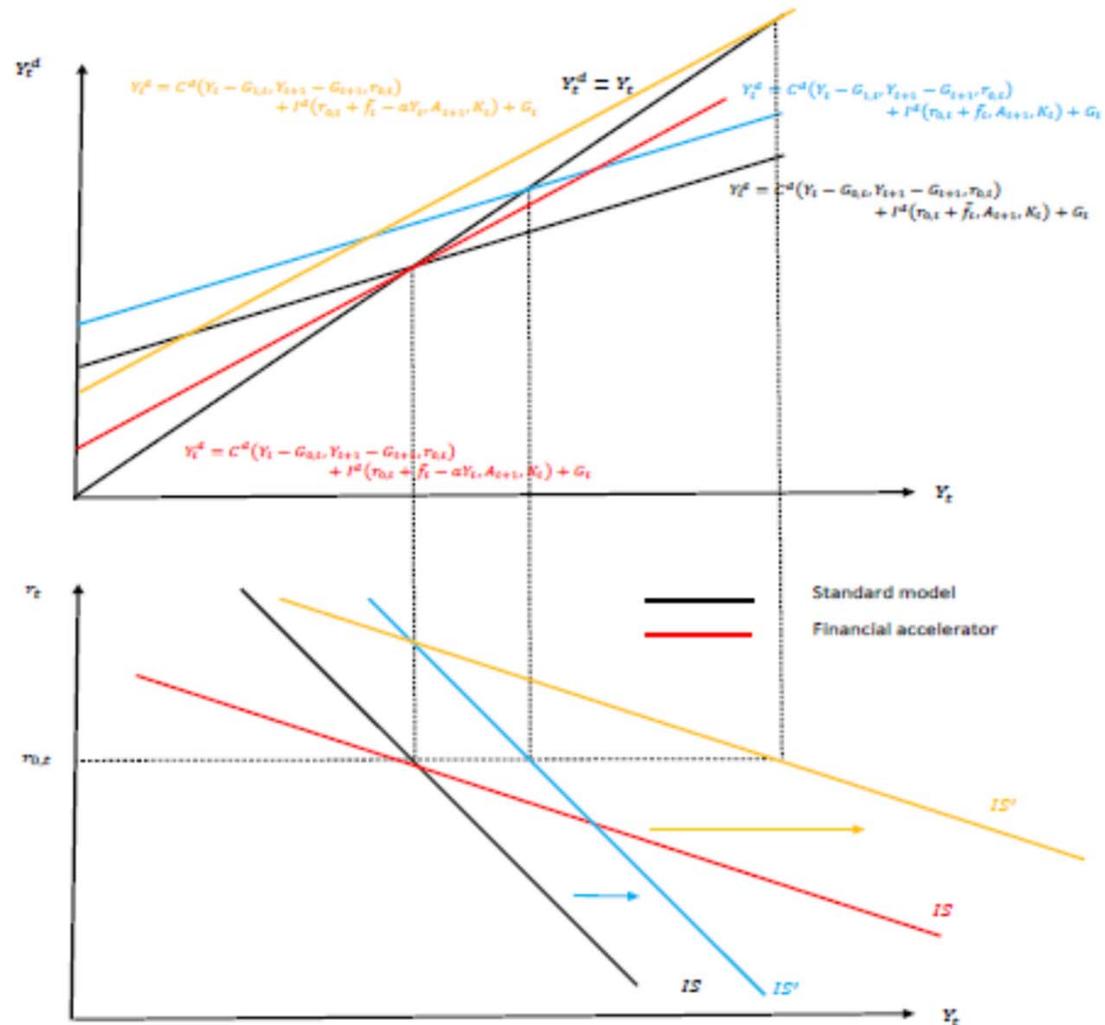
# Flatter AD Curve

Figure 35.5: The AD Curve with the Financial Accelerator



# Shift: Increase in G

Figure 35.6: Shift of the IS Curve with the Financial Accelerator



# IS-LM AD-AS

Figure 35.7: IS-LM-AD-AS Curves with Financial Accelerator

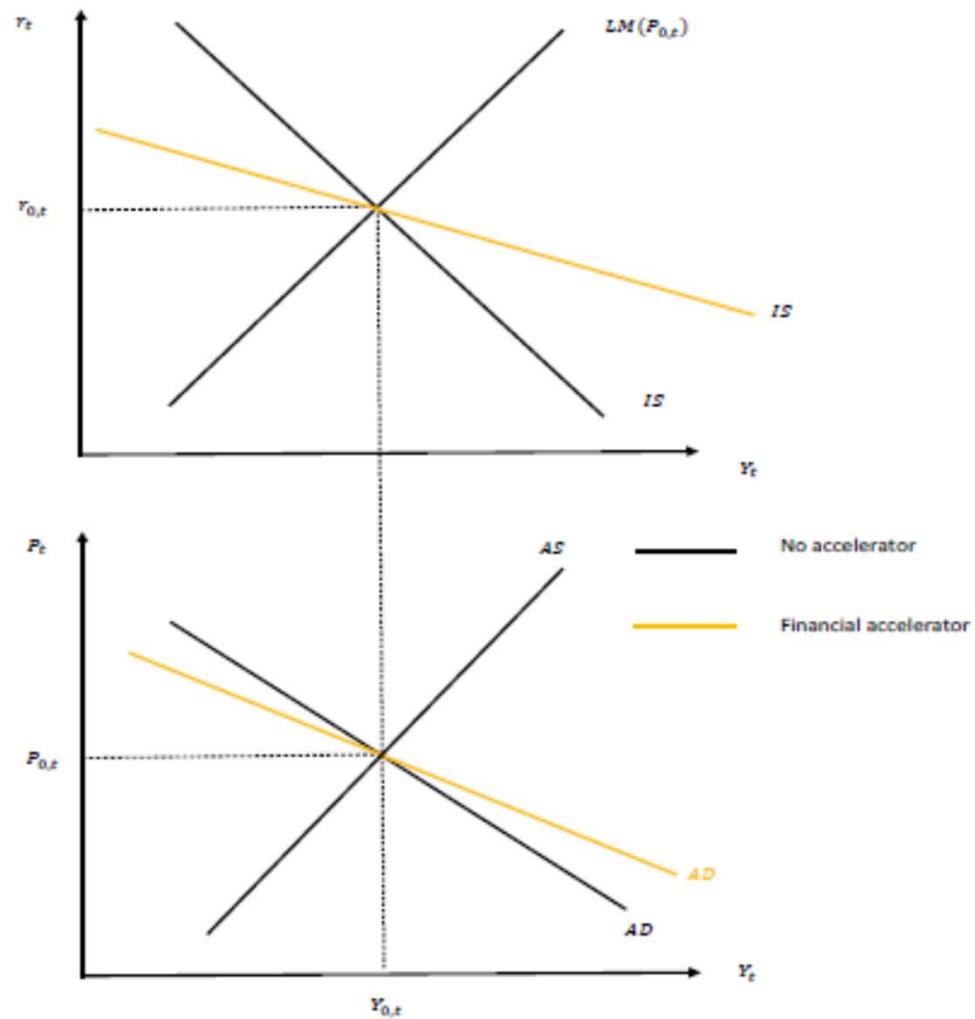


Figure 35.8: Supply Shock with Financial Accelerator

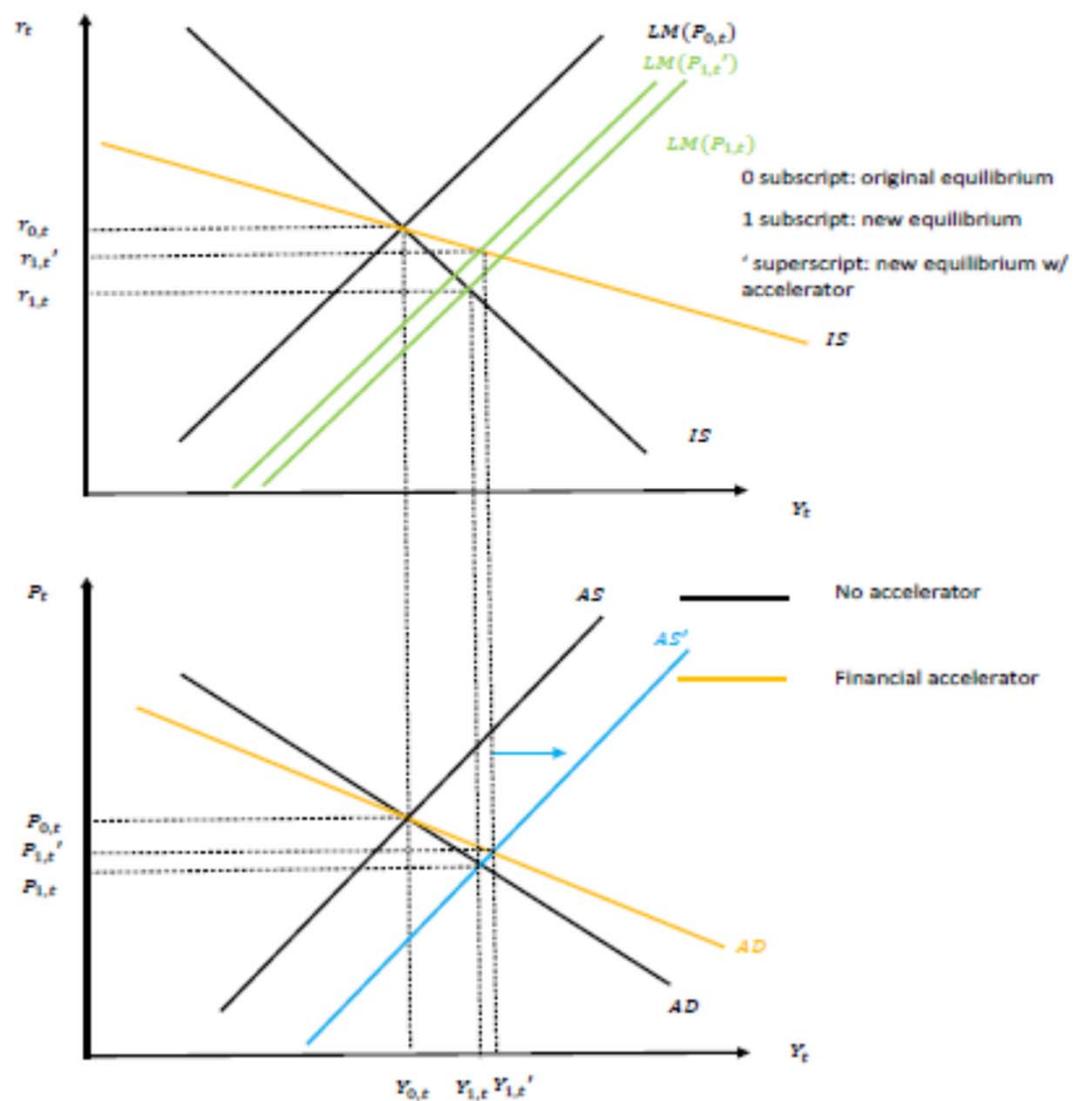
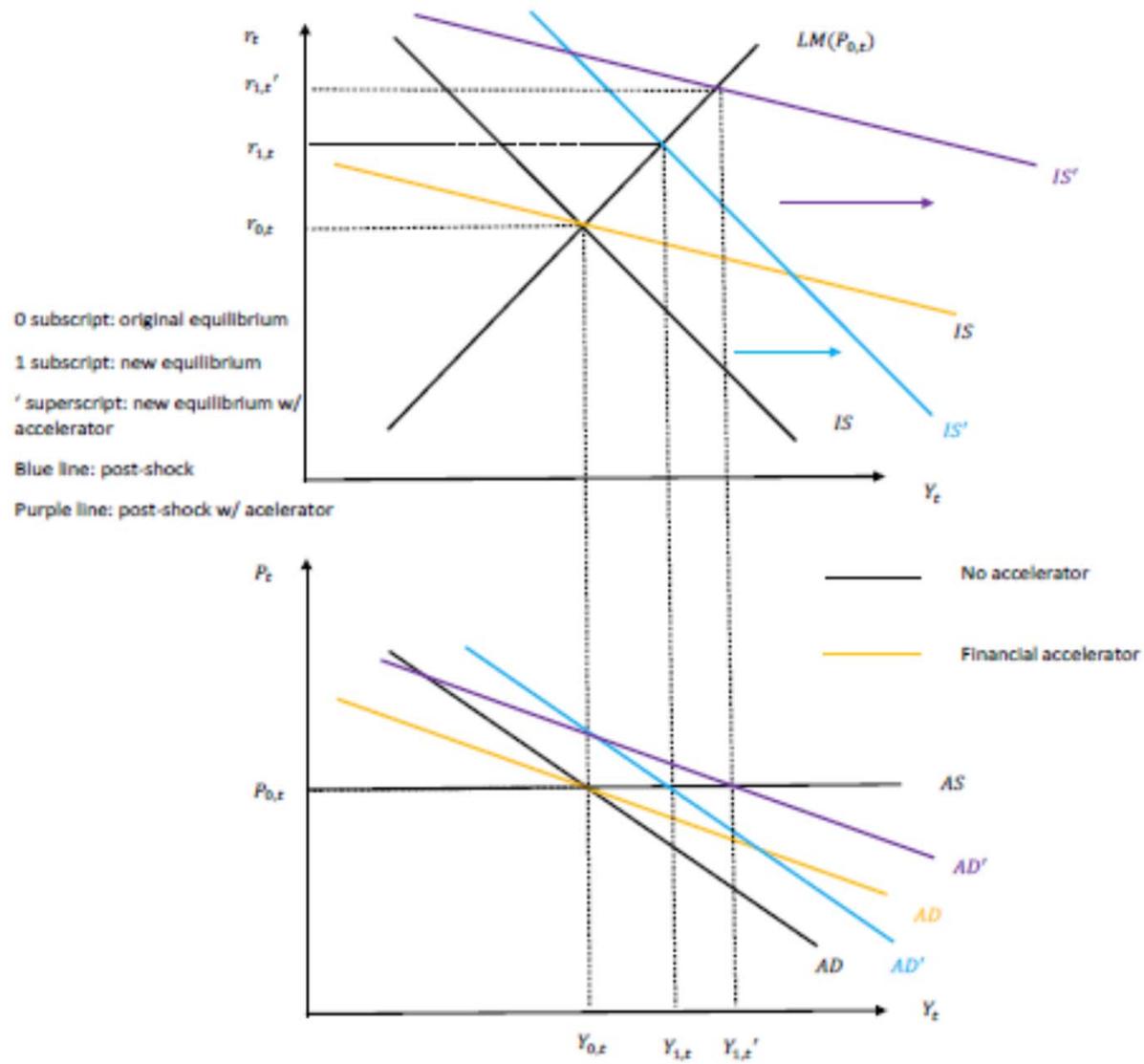


Figure 35.9: Demand Shock with Financial Accelerator, Simple Sticky Price Model



# Summary

- Financial structure only matters if there are frictions
- One friction – here assume firms borrow at higher rate than households
- Positive credit spread means equilibrium is not Pareto optimal
- Increase in  $f$  shifts in IS
- Defaults rise with economic weakness
- Financial accelerator flattens IS, AD
- And amplifies shocks