Economics 102
Spring 1998
Homework \#5 Answer Key
Due May 5(Tue) at the large lecture

Student Name:
ID\#:
T.A. Name:

Day/Time of Sec:

Question 1. (3 pts.)
a. (1 pt.) The FED sells $\$ 1,000$ of T-bills from a bank in Chicago. What will be the total change in the money supply if the reserve ratio is $25 \%$ ? Money multiplier $=\mathbf{1} / \mathbf{2 5}=\mathbf{4} \Rightarrow \Delta \mathbf{M s}=-\mathbf{\$ 1 0 0 0} * \mathbf{4}=\mathbf{\$ 4 , 0 0 0}$.
b. (1 pt.) The FED buys $\$ 2,000$ of T-bills on the open market. What will be the total change in the money supply if the reserve ratio is $25 \%$ ? Money multiplier $=\mathbf{1} / \mathbf{2 5}=\mathbf{4} \Rightarrow \Delta \mathrm{Ms}=\mathbf{\$ 2 0 0 0} * \mathbf{4}=\mathbf{\$ 8 , 0 0 0}$.
c. (1 pt.) Suppose David deposits his paycheck of $\$ 1,000$ in a bank in Green Bay. What will be the total change in money supply if the reserve ratio is $25 \%$ ? The increase in reserves at a bank in Green Bay will be equal to the decrease in reserves at David's employer's bank, so that $\Delta \mathbf{M s}=\mathbf{0}$.

Question 2. (7 pts.) Consider an economy where the required reserve ratio is $40 \%$. Suppose Mark sells $\$ 2,000$ worth of government securities to the FED and deposits the proceeds $(\$ 2,000)$ in Bank 1 . Note that this new deposit initially increases the quantity of money by $\$ 2,000$. Assume that all accounts were previously equal to 0 (or that we are only looking at changes), and there are no currency drains. After Mark has made his deposit, Bank 1's Balance Sheet is

Bank 1's Balance Sheet

| Asset | Liabilities |
| :--- | :--- |
| Reserves: $\$ 2,000$ | Demand Deposits: $\$ 2,000$ |

a. (2 pts.) Suppose that Bank 1 lends out any excess reserves to Jill. Jill uses the entire loan to buy a sofa from Tim, who deposits her payment in Bank 2. Fill in the following table for Bank 1 and Bank 2 immediately after Tim has deposited her payment. Be sure to label all entries.

| Bank 1's Balance Sheet |  |  |
| :--- | :--- | :--- |
| Asset | Liabilities |  |
| Reserves: $\mathbf{\$ 8 0 0}$ |  | Demand Deposits: \$2000 |
| Loans: $\mathbf{\$ 1 2 0 0}$ |  |  |

Bank 2's Balance Sheet

| Asset | Liabilities |
| :--- | :--- |
| Reserves: \$1200 | Demand Deposits: \$1200 |
|  |  |

b. (3 pts.) Suppose that Bank 2 lends out any excess reserves to Adam. Adam's entire loan ends up deposited in Bank 3, and so on. Fill in the following table.

| Bank <br> Number | New <br> Deposit | New <br> Loan | New <br> Reserve | Increase in <br> money | Cumulative <br> increase in <br> money |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | $\$ 2000$ | $\mathbf{\$ 1 2 0 0}$ | $\mathbf{\$ 8 0 0}$ | $\$ 2000$ | $\$ 2000$ |
| 2 | $\mathbf{1 2 0 0}$ | $\mathbf{7 2 0}$ | $\mathbf{4 8 0}$ | $\mathbf{1 2 0 0}$ | $\mathbf{3 2 0 0}$ |
| 3 | $\mathbf{4 3 2}$ | $\mathbf{4 3 2}$ | $\mathbf{2 8 8}$ | $\mathbf{7 2 0}$ | $\mathbf{3 9 2 0}$ |
| 4 | $:$ | $\mathbf{2 5 9 . 2}$ | $\mathbf{1 7 2 . 8}$ | $\mathbf{4 3 2}$ | $\mathbf{4 3 5 2}$ |
| $:$ | 0.000442 | 0.000265 | 0.000177 | 0.000442 | 4999.999 |
| 31 |  |  |  |  | $:$ |

c. (1 pt.) What is the money multiplier? Money multiplier $=1 /$ required reserve ratio=1/.4=2.5
d. (1 pt.) After all rounds have been completed, what will the total increase in money be?

Money multiplier $=\mathbf{2 . 5} \Rightarrow \Delta \mathrm{Ms}=\mathbf{\$ 2 0 0 0} \boldsymbol{2} .5=\mathbf{\$ 5 , 0 0 0}$.
Question 3. (10 pts.) Consider an economy with:
Money demand and supply are:
$\mathrm{Md}=5000-100 \mathrm{r}$
$\mathrm{Ms}=2500$

Output market is:
$\mathrm{C}=800+.8(\mathrm{Y}-\mathrm{T})-10 \mathrm{P}$
$\mathrm{I}=2000-40 \mathrm{r}$
$\mathrm{G}=2000$
$\mathrm{T}=1000$
where P is the aggregate price level and $\mathbf{r}$ is percentage interest rate(Not decimal term).
a. (1 pt.) Use the money market equations to find the equilibrium interest rate.
$\mathbf{M d}=5000-100 \mathrm{r}=\mathbf{2 5 0 0}=\mathbf{M s} \Rightarrow$ The equilibrium interest rate $=\mathbf{2 5}=\mathbf{2 5 \%}$
b. (1 pt.) Assume that $\mathrm{P}=200$. (Hint: This is a Keynesian model where the price level is fixed.) Using your answer to part(a), solve for the equilibrium GDP (Ye).
$\mathrm{Ye}=\mathrm{C}+\mathrm{I}+\mathrm{G}=800+.8(\mathrm{Ye}-1000)-10(200)+2000-40 * 25+2000$
$.2 \mathrm{Ye}=1000 \Rightarrow$ The equilibrium Output $=5000$
Now suppose aggregate demand (AD) and aggregate supply (AS) are given by (Hint: we are now allowing price to vary):

$$
\begin{aligned}
& \mathrm{AD}: \mathrm{Y}^{\mathrm{D}}=\mathrm{C}+\mathrm{I}+\mathrm{G} \\
& \mathrm{AS}: \mathrm{Y}^{\mathrm{S}}=100 \mathrm{P}, \text { or } \mathrm{P}=0.01 \mathrm{Y}^{\mathrm{S}}
\end{aligned}
$$

c. (1 pt.) Using your answer to part(a), find AD equation. (Hints: solve for $\mathrm{Y}^{\mathrm{D}}$ as a function of P , or P as a function of $\mathrm{Y}^{\mathrm{D}}$.)
$Y^{\mathrm{D}}=\mathrm{C}+\mathrm{I}+\mathrm{G}=800+.8(\mathrm{Ye}-1000)-10 \mathrm{P}+2000-40 * 25+2000$
$Y^{D}=15000-50 \mathrm{P}$, or $P=300-0.02 Y^{D}$.
d. (2 pts.) Using your answer to part(a) and (c), solve for the equilibrium GDP (Ye) and Price (P).

$$
\begin{aligned}
& Y^{D}=15000-50 P=100 P=Y^{S} \quad \Rightarrow Y e=10000 \text { and } P=100 . \\
& \text { Or } P=300-0.02 Y^{D}=0.01 Y^{S}=P \Rightarrow Y e=10000 \text { and } P=100 .
\end{aligned}
$$

e. (1 pt.) Suppose that the full employment level of GDP is 12500 . Does the current equilibrium GDP show an inflationary gap? It shows a recessionary gap.
f. (2 pts.) In order to reach the full employment level of GDP (i.e. Yfe $=12500$ ), government decides to change government spending. Then what will be new G? Does the equilibrium price increase or decrease? Why?
(Hint: Don't use multipliers.)

$$
\left.\begin{array}{rl}
\mathrm{Y}^{\mathrm{D}} & =\mathrm{C}+\mathrm{I}+\mathrm{G}=800+.8(\mathrm{Ye}-1000)-10 \mathrm{P}+2000-40 * 25+\mathrm{G} \\
& =5000+5 \mathrm{G}-50 \mathrm{P} \quad\left(\text { or } \mathrm{P}=100+.1 \mathrm{G}-0.02 \mathrm{Y}^{\mathrm{D}}\right)
\end{array}\right] \begin{aligned}
& \mathrm{P}=100+.1 \mathrm{G}-0.02 \mathrm{Y}^{\mathrm{D}}=0.01 \mathrm{Y}^{\mathrm{S}}=\mathrm{P} \\
& 100+.1 \mathrm{G}-\mathbf{0 . 0 2}(\mathbf{1 2 5 0 0})=0.01(\mathbf{1 2 5 0 0}) \Rightarrow \text { new } G=\mathbf{2 7 5 0} . \text { Because AD shifts out, } P \text { goes up. }
\end{aligned}
$$

g. (2 pts.) Alternatively, suppose the money supply (Ms) is set by the FED at $\$ 4375$ (and $G=2000$ ). Can we reach the full employment level of GDP (i.e. Yfe $=12500$ )? What is the new equilibrium price?

$$
\begin{aligned}
& \text { Md }=5000-100 \mathrm{r}=4375=\mathrm{Ms} \Rightarrow \text { The equilibrium interest rate }=6.25=6.25 \% \\
& \mathrm{Y}^{\mathrm{D}}=\mathrm{C}+\mathrm{I}+\mathrm{G}=800+.8(\mathrm{Ye}-1000)-10 \mathrm{P}+2000-40 * 6.25+2000=18750-50 \mathrm{P} \\
& \mathrm{Y}^{\mathrm{D}}=18750-50 \mathrm{P}=100 \mathrm{P}=\mathrm{Y}^{\mathrm{S}} \quad \Rightarrow \mathrm{Ye}=12500 \text { and } \mathrm{P}=125
\end{aligned}
$$

