# Regression Discontinuity 

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I will describe the basic ideas of RD, but ignore many of the details

Good references (and things I used in preparing this are):

- "Identification and Estimation of Treatment Effects with a Regression-Discontinuity Design," Hahn, Todd, and Van der Klaauw, EMA (2001)
- "Manipulation of the Running Variable in the Regression Discontinuity Design: A Density Test," McCrary, Journal of Econometrics (2008)
- "Regression Discontinuity Designs: A Guide to Practice," Imbens and Lemieux, Journal of Econometrics (2008)
- "Regression Discontinuity Designs in Economics," Lee and Lemiux, JEL (2010)

You can also find various Handbook chapters or Mostly Harmless Econometrics which might help as well

The idea of regression discontinuity goes way back, but it has gained in popularity in recent years

The basic idea is to recognize that in many circumstances policy rules vary at some cutoff point

To think of the simplest case suppose the treatment assignment rule is:

$$
T_{i}= \begin{cases}0 & X_{i}<x^{*} \\ 1 & x_{i} \geq x^{*}\end{cases}
$$

Many different rules work like this.
Examples:

- Whether you pass a test
- Whether you are eligible for a program
- Who wins an election
- Which school district you reside in
- Whether some punishment strategy is enacted
- Birth date for entering kindergarten

This last one should look pretty familiar-Angrist and Krueger's quarter of birth was essentially a regression discontinuity design

The key insight is that right around the cutoff we can think of people slightly above as identical to people slightly below

Formally we can write it the model as:

$$
Y_{i}=\alpha T_{i}+\varepsilon_{i}
$$

If

$$
E\left(\varepsilon_{i} \mid X_{i}=x\right)
$$

is continuous then the model is identified (actually all you really need is that it is continuous at $x=x^{*}$ )

To see it is identified not that

$$
\begin{aligned}
& \lim _{x \uparrow x^{*}} E\left(Y_{i} \mid X_{i}=x\right)=E\left(\varepsilon_{i} \mid X_{i}=x^{*}\right) \\
& \lim _{x \downarrow x^{*}} E\left(Y_{i} \mid X_{i}=x\right)=\alpha+E\left(\varepsilon_{i} \mid X_{i}=x^{*}\right)
\end{aligned}
$$

Thus

$$
\alpha=\lim _{x \downarrow x^{*}} E\left(Y_{i} \mid X_{i}=x\right)-\lim _{x \uparrow x^{*}} E\left(Y_{i} \mid X_{i}=x\right)
$$

Thats it

What I have described thus far is referred to as a "Sharp
Regression Discontinuity"
There is also something called a "Fuzzy Regression Discontinuity"

This occurs when rules are not strictly enforced
Examples

- Birth date to start school
- Eligibility for a program has other criterion
- Whether punishment kicks in (might be an appeal process)

This isn't a problem as long as

$$
\lim _{x \uparrow x^{*}} E\left(T_{i} \mid X_{i}=x\right)>\lim _{x \downarrow x^{*}} E\left(T_{i} \mid X_{i}=x\right)
$$

To see identification we now have

$$
\begin{aligned}
& \lim _{x \uparrow x^{*}} E\left(Y_{i} \mid X_{i}=x\right)-\lim _{x \downarrow x^{*}} E\left(Y_{i} \mid X_{i}=x\right) \\
& \lim _{x \uparrow x^{*}} E\left(T_{i} \mid X_{i}=x\right)-\lim _{x \downarrow x^{*}} E\left(T_{i} \mid X_{i}=x\right) \\
& =\frac{\alpha\left[\lim _{x \uparrow x^{*}} E\left(T_{i} \mid X_{i}=x\right)-\lim _{x \downarrow x^{*}} E\left(T_{i} \mid X_{i}=x\right)\right]}{\lim _{x \uparrow x^{*}} E\left(T_{i} \mid X_{i}=x\right)-\lim _{x \downarrow x^{*}} E\left(T_{i} \mid X_{i}=x\right)} \\
& =\alpha
\end{aligned}
$$

Note that this is essentially just Instrumental variables (this is often referred to as the Wald Estimator)

You can also see that this works when $T_{i}$ is continuous

## How do we do this in practice?

There are really two approaches.
The first comes from the basic idea of identification, we want to look directly to the right and directly to the left of the policy change

Lets focus on the Sharp case-we can get the fuzzy case by just applying to $Y_{i}$ and $T_{i}$ and then taking the ratio

The data should look something like this (in stata)

We can think about estimating the end of the red line and the end of the green line and taking the difference

This is basically just a version of nonparametric regression at these two points

Our favorite way to estimate nonparametric regression in economics is by Kernel regression

Let $K(x)$ be a kernel that is positive and non increasing in $|x|$ and is zero when $|x|$ is large

Examples:

- Normal pdf: $\exp \left(-x^{2}\right)$ Normal
- Absolute value: Absolute

$$
\begin{cases}1-|x| & |x|<1 \\ 0 & |x| \geq 1\end{cases}
$$

- Uniform: $1(|x|<1)$ Uniform
- Epanechnikov kernel: Epanechnikov

$$
\begin{cases}\frac{3}{4}\left(1-u^{2}\right) & |x|<1 \\ 0 & |x| \geq 1\end{cases}
$$

The kernel regressor is defined as

$$
E(Y \mid X=x) \approx \frac{\sum_{i=1}^{N} K\left(\frac{x_{i}-x}{h}\right) Y_{i}}{\sum_{i=1}^{N} K\left(\frac{X_{i}-X}{h}\right)}
$$

where $h$ is the bandwidth parameter
Note that this is just a weighted average

- it puts higher weight on observations closer to $x$
- when $h$ is really big we put equal weight on all observations
- when $h$ is really small, only the observations that are very close to $x$ influence it

This is easiest to think about with the uniform kernel
In this case

$$
K\left(\frac{X_{i}-x}{h}\right)=1\left(\left|X_{i}-x\right|<h\right)
$$

So we use take a simple sample mean of observations within $h$ units of $X_{i}$

Clearly in this case as with other kernels, as the sample size goes up, $h$ goes down so that asymptotically we are only putting weight on observations very close to $x$

To estimate $\lim _{x \downarrow x^{*}} E\left(T_{i} \mid X_{i}=x\right)$ we only want to use values of $X_{i}$ to the right of $x^{*}$, so we would use

$$
\lim _{x \downarrow x^{*}} E\left(T_{i} \mid X_{i}=x\right) \approx \frac{\sum_{i=1}^{N} 1\left(X_{i}>x^{*}\right) K\left(\frac{X_{i}-x^{*}}{h}\right) Y_{i}}{\sum_{i=1}^{N} 1\left(X_{i}>x^{*}\right) K\left(\frac{X_{i}-x^{*}}{h}\right)}
$$

However it turns out that this has really bad properties because we are looking at the end point

For example suppose the data looked like this



For any finite bandwidth the estimator would be biased downward

It is better to use local linear (or polynomial) regression.
Here we choose
$(\hat{a}, \hat{b})=\operatorname{argmin}_{a, b} \sum_{i=1}^{N} K\left(\frac{X_{i}-x^{*}}{h}\right)\left[Y_{i}-a-b\left(X_{i}-x^{*}\right)\right]^{2} 1\left(X_{i} \geq x^{*}\right)$
Then the estimate of the right hand side is $\widehat{a}$.
We do the analogous thing on the other side:
$(\hat{a}, \hat{b})=\operatorname{argmin}_{a, b} \sum_{i=1}^{N} K\left(\frac{X_{i}-x^{*}}{h}\right)\left[Y_{i}-a-b\left(X_{i}-x^{*}\right)\right]^{2} 1\left(X_{i}<x^{*}\right)$
(which with a uniform kernel just means running a regression using the observations between $x^{*}-h$ and $x^{*}$

Lets try this in stata

There is another approach to estimating the model
Define

$$
g(x)=E\left(\varepsilon_{i} \mid X_{i}=x\right)
$$

then

$$
E\left(Y_{i} \mid X_{i}, T_{i}\right)=\alpha T_{i}+g\left(X_{i}\right)
$$

where $g$ is a smooth function
Thus we can estimate the model by writing down a smooth flexible functional form for $g$ and just estimate this by OLS

The most obvious functional form that people use is a polynomial

There are really two different ways to do it:

$$
Y_{i}=\alpha T_{i}+b_{0}+b_{1} X_{i}+b_{2} X_{i}^{2}+v_{i}
$$

or

$$
\begin{aligned}
Y_{i}= & \alpha T_{i}+b_{0}+b_{1} X_{i} 1\left(X_{i}<x\right)+b_{2} X_{i}^{2} 1\left(X_{i}<x\right) \\
& +b_{3} X_{i} 1\left(X_{i} \geq x\right)+b_{4} X_{i}^{2} 1\left(X_{i} \geq x\right)+v_{i}
\end{aligned}
$$

Lee and Lemieux say the second is better

Note that this is just as "nonparametric" as the Kernel approach

- You must promise to increase the degree of the polynomial as you increase the sample size (in the same way that you lower the bandwidth with the sample size)
- You still have a practical problem of how to choose the degree of the polynomial (in the same way you have a choice about how to choose the bandwidth in the kernel approaches)

You can do both and use a local polynomial-in one case you promise to lower the bandwidth, in the other you promise to add more terms, you could do both

Also, for the "fuzzy" design we can just do IV

## Problems

While RD is often really nice, there are three major problems that arise

The first is kind of obvious from what we are doing-and is an estimation problem rather than an identification problem

Often the sample size is not very big and as a practical matter the bandwidth is so large (or the degree of the polynomial so small) that it isn't really regression discontinuity that is identifying things

The second problem is that there may be other rules changes happening at the same cutoff so you aren't sure what exactly you are identifying

One suggestion to test for this is to look at observable characteristics

The third is if the running variable is endogenous
Clearly if people choose $X_{i}$ precisely the whole thing doesn't work

For example suppose

- carrying 1 pound of drugs was a felony, but less than 1 was a misdemeanor
- people who get their paper in by 5:00 on thursday afternoon are on time, 5:01 is late and marked down by a grade

Note that you need $X_{i}$ to be precisely manipulated, if there is still some randomness on the actual value of $X_{i}$, rd looks fine

Mccrary (2008) suggests to test for this by looking at the density around the cutoff point:

- Under the null the density should be continuous at the cutoff point
- Under the alternative, the density would increase at the kink point when $T_{i}$ is viewed as a good thing

Lets look at some examples

## Randomized Experiments from Non-random Selection in U.S. House Elections

Lee, Journal of Econometrics, 2008
One of the main points of this paper is that the running variable can be endogenous as long as it can not be perfectly chosen.

In particular it could be that:

$$
X_{i}=W_{i}+\xi_{i}
$$

where $W_{i}$ is chosen by someone, but $\xi_{i}$ is random and unknown when $W_{i}$ is chosen

Lee shows that regression discontinuity approaches still work in this case

## Incumbency

We can see that incumbents in congress are re-elected at very high rates

Is this because there is an effect of incumbency or just because of serial correlation in preferences?

Regression discontinuity helps solves this problem-look at people who just barely won (or lost).

a


Democratic Vote Share Margin of Victory, Election $t$ h

## a


a


Table 1
Electoral outcomes and pre-determined election characteristics: democratic candidates, winners vs. losers: 1948-1996

| Variable | All |  | $\mid$ Margin $\mid<.5$ |  | $\mid$ Margin $\mid<.05$ |  | Parametric fit |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Winner | Loser | Winner | Loser | Winner | Loser | Winner | Loser |
| Democrat vote share election $t+1$ | $\begin{aligned} & 0.698 \\ & (0.003) \\ & {[0.179]} \end{aligned}$ | $\begin{aligned} & 0.347 \\ & (0.003) \\ & {[0.15]} \end{aligned}$ | $\begin{aligned} & 0.629 \\ & (0.003) \\ & {[0.145]} \end{aligned}$ | $\begin{aligned} & 0.372 \\ & (0.003) \\ & {[0.124]} \end{aligned}$ | $\begin{aligned} & 0.542 \\ & (0.006) \\ & {[0.116]} \end{aligned}$ | $\begin{aligned} & 0.446 \\ & (0.006) \\ & {[0.107]} \end{aligned}$ | $\begin{aligned} & 0.531 \\ & (0.008) \end{aligned}$ | $\begin{aligned} & 0.454 \\ & (0.008) \end{aligned}$ |
| Democrat win prob. election $t+1$ | $\begin{aligned} & 0.909 \\ & (0.004) \\ & {[0.276]} \end{aligned}$ | $\begin{aligned} & 0.094 \\ & (0.005) \\ & {[0.285]} \end{aligned}$ | $\begin{aligned} & 0.878 \\ & (0.006) \\ & {[0.315]} \end{aligned}$ | $\begin{aligned} & 0.100 \\ & (0.006) \\ & {[0.294]} \end{aligned}$ | $\begin{aligned} & 0.681 \\ & (0.026) \\ & {[0.458]} \end{aligned}$ | $\begin{aligned} & 0.202 \\ & (0.023) \\ & {[0.396]} \end{aligned}$ | $\begin{aligned} & 0.611 \\ & (0.039) \end{aligned}$ | $\begin{aligned} & 0.253 \\ & (0.035) \end{aligned}$ |
| Democrat vote share election $t-1$ | $\begin{aligned} & 0.681 \\ & (0.003) \\ & {[0.189]} \end{aligned}$ | $\begin{aligned} & 0.368 \\ & (0.003) \\ & {[0.153]} \end{aligned}$ | $\begin{aligned} & 0.607 \\ & (0.003) \\ & {[0.152]} \end{aligned}$ | $\begin{aligned} & 0.391 \\ & (0.003) \\ & {[0.129]} \end{aligned}$ | $\begin{aligned} & 0.501 \\ & (0.007) \\ & {[0.129]} \end{aligned}$ | $\begin{aligned} & 0.474 \\ & (0.008) \\ & {[0.133]} \end{aligned}$ | $\begin{aligned} & 0.477 \\ & (0.009) \end{aligned}$ | $\begin{aligned} & 0.481 \\ & (0.01) \end{aligned}$ |
| Democrat win prob. election $t-1$ | $\begin{aligned} & 0.889 \\ & (0.005) \\ & {[0.31]} \end{aligned}$ | $\begin{aligned} & 0.109 \\ & (0.006) \\ & {[0.306]} \end{aligned}$ | $\begin{aligned} & 0.842 \\ & (0.007) \\ & {[0.36]} \end{aligned}$ | $\begin{aligned} & 0.118 \\ & (0.007) \\ & {[0.317]} \end{aligned}$ | $\begin{aligned} & 0.501 \\ & (0.027) \\ & {[0.493]} \end{aligned}$ | $\begin{aligned} & 0.365 \\ & (0.028) \\ & {[0.475]} \end{aligned}$ | $\begin{aligned} & 0.419 \\ & (0.038) \end{aligned}$ | $\begin{aligned} & 0.416 \\ & (0.039) \end{aligned}$ |
| Democrat political experience | $\begin{aligned} & 3.812 \\ & (0.061) \\ & {[3.766]} \end{aligned}$ | $\begin{aligned} & 0.261 \\ & (0.025) \\ & {[1.293]} \end{aligned}$ | $\begin{aligned} & 3.550 \\ & (0.074) \\ & {[3.746]} \end{aligned}$ | $\begin{aligned} & 0.304 \\ & (0.029) \\ & {[1.39]} \end{aligned}$ | $\begin{aligned} & 1.658 \\ & (0.165) \\ & {[2.969]} \end{aligned}$ | $\begin{aligned} & 0.986 \\ & (0.124) \\ & {[2.111]} \end{aligned}$ | $\begin{aligned} & 1.219 \\ & (0.229) \end{aligned}$ | $\begin{aligned} & 1.183 \\ & (0.145) \end{aligned}$ |
| Opposition political experience | $\begin{aligned} & 0.245 \\ & (0.018) \\ & {[1.084]} \end{aligned}$ | $\begin{aligned} & 2.876 \\ & (0.054) \\ & {[2.802]} \end{aligned}$ | $\begin{aligned} & 0.350 \\ & (0.025) \\ & {[1.262]} \end{aligned}$ | $\begin{aligned} & 2.808 \\ & (0.057) \\ & {[2.775]} \end{aligned}$ | $\begin{aligned} & 1.183 \\ & (0.118) \\ & {[2.122]} \end{aligned}$ | $\begin{aligned} & 1.345 \\ & (0.115) \\ & {[1.949]} \end{aligned}$ | $\begin{aligned} & 1.424 \\ & (0.131) \end{aligned}$ | $\begin{aligned} & 1.293 \\ & (0.17) \end{aligned}$ |
| Democrat electoral experience | $\begin{aligned} & 3.945 \\ & (0.061) \\ & {[3.787]} \end{aligned}$ | $\begin{aligned} & 0.464 \\ & (0.028) \\ & {[1.457]} \end{aligned}$ | $\begin{aligned} & 3.727 \\ & (0.075) \\ & {[3.773]} \end{aligned}$ | $\begin{aligned} & 0.527 \\ & (0.032) \\ & {[1.55]} \end{aligned}$ | $\begin{aligned} & 1.949 \\ & (0.166) \\ & {[2.986]} \end{aligned}$ | $\begin{aligned} & 1.275 \\ & (0.131) \\ & {[2.224]} \end{aligned}$ | $\begin{aligned} & 1.485 \\ & (0.23) \end{aligned}$ | $\begin{aligned} & 1.470 \\ & (0.151) \end{aligned}$ |
| Opposition electoral experience | $\begin{aligned} & 0.400 \\ & (0.019) \\ & {[1.189]} \end{aligned}$ | $\begin{aligned} & 3.007 \\ & (0.054) \\ & {[2.838]} \end{aligned}$ | $\begin{aligned} & 0.528 \\ & (0.027) \\ & {[1.357]} \end{aligned}$ | $\begin{aligned} & 2.943 \\ & (0.058) \\ & {[2.805]} \end{aligned}$ | $\begin{aligned} & 1.375 \\ & (0.12) \\ & {[2.157]} \end{aligned}$ | $\begin{aligned} & 1.529 \\ & (0.119) \\ & {[2.022]} \end{aligned}$ | $\begin{aligned} & 1.624 \\ & (0.132) \end{aligned}$ | $\begin{aligned} & 1.502 \\ & (0.174) \end{aligned}$ |
| Observations | 3818 | 2740 | 2546 | 2354 | 322 | 288 | 3818 | 2740 |

## Table 2

Effect of winning an election on subsequent party electoral success: alternative specifications, and refutability test, regression discontinuity estimates

| Dependent variable (1) | $(2)$ | $(3)$ | $(4)$ | $(5)$ | $(6)$ | $(8)$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | Vote share | Vote share | Vote share | Vote share | Vote share | Res. vote share |
|  | $t+1$ |  |  |  |  |  |

## Maimonides' Rule

Angrist and Lavy look at the effects of school class size on kid's outcomes

Maimonides was a twelfth century Rabbinic scholar
He interpreted the Talmud in the following way:

> Twenty-five children may be put it charge of one teacher. If the number in the class exceeds twenty-five but is not more than forty, he should have an assistant to help with the instruction. If there are more than forty, two teachers must be appointed.

This rule has had a major impact on education in Israel
They try to follow this rule so that no class has more than 40 kids

But this means that

- If you have 80 kids in a grade, you have two classes with 40 each
- if you have 81 kids in a grade, you have three classes with 27 each

That sounds like a regression discontinuity
We can write the rule as

$$
f_{s c}=\frac{e_{s}}{\left[\operatorname{int}\left(\frac{e_{s}-1}{40}\right)+1\right]}
$$

Ideally we could condition on grades with either 80 or 81 kids
More generally there are two ways to do this

- condition on people close to the cutoff and use $f_{s c}$ as an instrument
- Control for class size in a "smooth" way and use $f_{s c}$ as an instrument

| Variable | Mean | S.D. | Quantiles |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 0.10 | 0.25 | 0.50 | 0.75 | 0.90 |
| A. Full sample |  |  |  |  |  |  |  |
| 5 th grade (2019 classes, 1002 schools, tested in 1991) |  |  |  |  |  |  |  |
| Class size | 29.9 | 6.5 | 21 | 26 | 31 | 35 | 38 |
| Enrollment | 77.7 | 38.8 | 31 | 50 | 72 | 100 | 128 |
| Percent disadvantaged | 14.1 | 13.5 | 2 | 4 | 10 | 20 | 35 |
| Reading size | 27.3 | 6.6 | 19 | 23 | 28 | 32 | 36 |
| Math size | 27.7 | 6.6 | 19 | 23 | 28 | 33 | 36 |
| Average verbal | 74.4 | 7.7 | 64.2 | 69.9 | 75.4 | 79.8 | 83.3 |
| Average math | 67.3 | 9.6 | 54.8 | 61.1 | 67.8 | 74.1 | 79.4 |
| 4th grade (2049 classes, 1013 schools, tested in 1991) |  |  |  |  |  |  |  |
| Class size | 30.3 | 6.3 | 22 | 26 | 31 | 35 | 38 |
| Enrollment | 78.3 | 37.7 | 30 | 51 | 74 | 101 | 127 |
| Percent disadvantaged | 13.8 | 13.4 | 2 | 4 | 9 | 19 | 35 |
| Reading size | 27.7 | 6.5 | 19 | 24 | 28 | 32 | 36 |
| Math size | 28.1 | 6.5 | 19 | 24 | 29 | 33 | 36 |
| Average verbal | 72.5 | - 8.0 | 62.1 | 67.7 | 73.3 | 78.2 | 82.0 |
| Average math | 68.9 | 8.8 | 57.5 | 63.6 | 69.3 | 75.0 | 79.4 |
| 3 r grade ( 2111 classes, 1011 schools, tested in 1992) |  |  |  |  |  |  |  |
| Class size | 30.5 | 6.2 | 22 | 26 | 31 | 35 | 38 |
| Enrollment | 79.6 | 37.3 | 34 | 52 | 74 | 104 | 129 |
| Percent disadvantaged | 13.8 | 13.4 | 2 | 4 | 9 | 19 | 35 |
| Reading size | 24.5 | 5.4 | 17 | 21 | 25 | 29 | 31 |
| Math size | 24.7 | 5.4 | 18 | 21 | 25 | 29 | 31 |
| Average verbal | 86.3 | 6.1 | 78.4 | 83.0 | 87.2 | 90.7 | 93.1 |
| Average math | 84.1 | 6.8 | 75.0 | 80.2 | 84.7 | 89.0 | 91.9 |

B. $+/-5$ Discontinuity sample (enrollment $36-45,76-85,116-124$ )

|  | 5 th grade |  | 4th grade |  | 3 rd grade |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mean | S.D. | Mean | S.D. | Mean | S.D. |
|  | (471 classes, 224 schools) |  | (415 classes, 195 schools |  | (441 classes, 206 schools) |  |
| Class size | 30.8 | 7.4 | 31.1 | 7.2 | 30.6 | 7.4 |
| Enrollment | 76.4 | 29.5 | 78.5 | 30.0 | 75.7 | 28.2 |
| Percent disadvantaged | 13.6 | 13.2 | 12.9 | 12.3 | 14.5 | 14.6 |
| Reading size | 28.1 | 7.3 | 28.3 | 7.7 | 24.6 | 6.2 |
| Math size | 28.5 | 7.4 | 28.7 | 7.7 | 24.8 | 6.3 |
| Average verbal | 74.5 | 8.2 | 72.5 | 7.8 | 86.2 | 6.3 |
| Average math | 67.0 | 10.2 | 68.7 | 9.1 | 84.2 | 7.0 |

[^0] September grade enrollment, Percent disadvantaged $=$ percent of students in the school from disadvantage backgrounds," Reading size $=$ number of students who took the reading test, Math size $=$ number of student who took the math test, Average verbal = average composite reading score in the class, Average math average composite math score in the class.
a. Fifth Grade

b. Fourth Grade

a. Fifth Grade

b. Fourth Grade


To estimate the model they use an econometric framework

$$
Y_{i c s}=\beta_{0}+\beta_{1} C_{c s}+\beta_{2} X_{i c s}+\alpha_{s}+\varepsilon_{i c s}
$$

Now we can't just put in a school effect because we will loose too much variation so think of $\alpha_{s}$ as part of the error term

Their data is a bit different because it is by class rather than by individual-but for this that isn't a big deal

Angrist and Lavy first estimate this model by OLS to show what we would get

TABLE II
OLS Estimates for 1991

|  | 5th Grade |  |  |  |  |  | 4th Grade |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Reading comprehension |  |  | Math |  |  | Reading comprehension |  |  | Math |  |  |
|  | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) |
| Mean score (s.d.) |  | 74.3 $(8.1)$ |  |  | 67.3 $(9.9)$ |  | $72.5$ |  |  | 69.9 |  |  |
| Regressors |  |  |  |  |  |  |  |  |  |  |  |  |
| Class size | $\begin{gathered} .221 \\ (.031) \end{gathered}$ | $\begin{gathered} -.031 \\ (.026) \end{gathered}$ | $\begin{gathered} -.025 \\ (.031) \end{gathered}$ | $\begin{gathered} .322 \\ (.039) \end{gathered}$ | $\begin{gathered} .076 \\ (.036) \end{gathered}$ | $\begin{gathered} .019 \\ (.044) \end{gathered}$ | $\begin{gathered} 0.141 \\ (.033) \end{gathered}$ | $\begin{gathered} -.053 \\ (.028) \end{gathered}$ | $\begin{gathered} -.040 \\ (.033) \end{gathered}$ | $\begin{gathered} .221 \\ (.036) \end{gathered}$ | $\begin{gathered} .055 \\ (.033) \end{gathered}$ | $\begin{gathered} .009 \\ (.039) \end{gathered}$ |
| Percent disadvantaged |  | $\begin{gathered} -.350 \\ (.012) \end{gathered}$ | $\begin{gathered} -.351 \\ (.013) \end{gathered}$ |  | $\begin{gathered} -.340 \\ (.018) \end{gathered}$ | $\begin{gathered} -.332 \\ (.018) \end{gathered}$ |  | $\begin{gathered} -.339 \\ (.013) \end{gathered}$ | $\begin{gathered} -.341 \\ (.014) \end{gathered}$ |  | $\begin{gathered} -.289 \\ (.016) \end{gathered}$ | $\begin{array}{r} -.281 \\ (.016) \end{array}$ |
| Enrollment |  |  | $\begin{gathered} -.002 \\ (.006) \end{gathered}$ |  |  | $\begin{gathered} .017 \\ (.009) \end{gathered}$ |  |  | $\begin{gathered} -.004 \\ (.007) \end{gathered}$ |  |  | $\begin{gathered} .014 \\ (.008) \end{gathered}$ |
| Root MSE | 7.54 | 6.10 | 6.10 | 9.36 | 8.32 | 8.30 | 7.94 | 6.65 | 6.65 | 8.66 | 7.82 | 7.81 |
| $R^{2}$ | . 036 | . 369 | . 369 | . 048 | . 249 | . 252 | . 013 | . 309 | . 309 | . 025 | . 204 | . 207 |
| N |  | 2,019 |  |  | 2,018 |  |  | 2,049 |  |  | 2,049 |  |

The unit of observation is the average score in the class. Standard errors are reported in parentheses. Standard errors were corrected for within-school correlation between classes.

Next, they want to worry about the fact that $C_{C S}$ is correlated with $\alpha_{s}+\varepsilon_{\text {ics }}$

They run instrumental variables using $f_{s c}$ as an instrument.

TABLE IV
2SLS Estimates for 1991 (Fifth Graders)

|  | Reading comprehension |  |  |  |  |  | Math |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Full sample |  |  |  | $+/-5$ <br> Discontinuity sample |  | Full sample |  |  |  | $+/-5$ <br> Discontinuity sample |  |
|  | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) |
| Mean score (s.d.) | $\begin{aligned} & 74.4 \\ & (7.7) \end{aligned}$ |  |  |  | $\begin{aligned} & 74.5 \\ & (8.2) \end{aligned}$ |  | $\begin{aligned} & 67.3 \\ & (9.6) \end{aligned}$ |  |  |  | $\begin{gathered} 67.0 \\ (10.2) \end{gathered}$ |  |
| Regressors |  |  |  |  |  |  |  |  |  |  |  |  |
| Class size | $\begin{gathered} -.153 \\ (.040) \end{gathered}$ | $\begin{array}{r} -.275 \\ (.066) \end{array}$ | $\begin{gathered} -.260 \\ (.081) \end{gathered}$ | $\begin{array}{r} -.186 \\ (.104) \end{array}$ | $\begin{gathered} -.410 \\ (.113) \end{gathered}$ | $\begin{gathered} -.582 \\ (.181) \end{gathered}$ | $\begin{gathered} -.013 \\ (.056) \end{gathered}$ | $\begin{gathered} -.230 \\ (.092) \end{gathered}$ | $\begin{gathered} -.261 \\ (.113) \end{gathered}$ | $\begin{array}{r} -.202 \\ (.131) \end{array}$ | $\begin{gathered} -.185 \\ (.151) \end{gathered}$ | $\begin{gathered} -.443 \\ (.236) \end{gathered}$ |
| Percent disadvantaged | $\begin{gathered} -.372 \\ (.014) \end{gathered}$ | $\begin{gathered} -.369 \\ (.014) \end{gathered}$ | $\begin{gathered} -.369 \\ (.013) \end{gathered}$ |  | $\begin{gathered} -.477 \\ (.037) \end{gathered}$ | $\begin{gathered} -.461 \\ (.037) \end{gathered}$ | $\begin{gathered} -.355 \\ (.019) \end{gathered}$ | $\begin{gathered} -.350 \\ (.019) \end{gathered}$ | $\begin{gathered} -.350 \\ (.019) \end{gathered}$ |  | $\begin{gathered} -.459 \\ (.049) \end{gathered}$ | $\begin{gathered} -.435 \\ (.049) \end{gathered}$ |
| Enrollment |  | $\begin{gathered} .022 \\ (.009) \end{gathered}$ | $\begin{gathered} .012 \\ (.026) \end{gathered}$ |  |  | $\begin{gathered} .053 \\ (.028) \end{gathered}$ |  | $\begin{gathered} .041 \\ (.012) \end{gathered}$ | $\begin{gathered} .062 \\ (.037) \end{gathered}$ |  |  | $\begin{gathered} .079 \\ (.036) \end{gathered}$ |
| Enrollment squared/100 |  |  | $\begin{gathered} .005 \\ (.011) \end{gathered}$ |  |  |  |  |  | $\begin{gathered} -.010 \\ (.016) \end{gathered}$ |  | , |  |
| Piecewise linear trend |  |  |  | $\begin{aligned} & .136 \\ & (.032) \end{aligned}$ |  |  |  |  |  | $\begin{gathered} .193 \\ (.040) \end{gathered}$ |  |  |
| Root MSE | 6.15 | 6.23 | 6.22 | 7.71 | 6.79 | 7.15 | 8.34 | 8.40 | 8.42 | 9.49 | 8.79 | 9.10 |
| N |  | 2019 |  | 1961 |  | 1 |  | 2018 |  | 1960 |  |  |

[^1]
## Do Better Schools Matter? Parental Valuation of Elementary Education

Sandra Black, QJE, 1999
In the Tiebout model parents can "buy" better schools for their children by living in a neighborhood with better public schools

How do we measure the willingness to pay?
Just looking in a cross section is difficult: Richer parents probably live in nicer areas that are better for many reasons

Black uses the school border as a regression discontinuity
We could take two families who live on opposite side of the same street, but are zoned to go to different schools

The difference in their house price gives the willingness to pay for school quality.


Figure I
Example of Data Collection for One City: Melrose Streets, and Attendance District Boundaries
(Adjusted Standard Errors Are in Parentheses ${ }^{\text {b }}$ )
Dependent Variable $=\ln$ (house pŘice)

| Distance from boundary: | (1) <br> All houses ${ }^{\text {d }}$ | (2) <br> 0.35 mile from boundary (616 yards) | (3) <br> 0.20 mile from boundary (350 yards) | (4) <br> 0.15 mile from boundary (260 yards) | (5) <br> 0.15 mile from boundary (260 yards) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Elementary school test score ${ }^{\text {c }}$ | $\begin{gathered} .035 \\ (.004) \end{gathered}$ | $\begin{gathered} .016 \\ (.007) \end{gathered}$ | $\begin{aligned} & .013 \\ & (.0065) \end{aligned}$ | $\begin{gathered} .015 \\ (.007) \end{gathered}$ | $\begin{gathered} .031 \\ (.006) \end{gathered}$ |
| Bedrooms | $\begin{gathered} .033 \\ (.004) \end{gathered}$ | $\begin{gathered} .038 \\ (.005) \end{gathered}$ | $\begin{gathered} .037 \\ (.006) \end{gathered}$ | $\begin{gathered} .033 \\ (.007) \end{gathered}$ | $\begin{gathered} .035 \\ (.007) \end{gathered}$ |
| Bathrooms | $\begin{gathered} .147 \\ (.014) \end{gathered}$ | $\begin{gathered} .143 \\ (.018) \end{gathered}$ | $\begin{gathered} .135 \\ (.024) \end{gathered}$ | $\begin{gathered} .167 \\ (.027) \end{gathered}$ | $\begin{aligned} & .193 \\ & (.028) \end{aligned}$ |
| Bathrooms squared | $\begin{gathered} -.013 \\ (.003) \end{gathered}$ | $\begin{gathered} -.017 \\ (.004) \end{gathered}$ | $\begin{gathered} -.015 \\ (.005) \end{gathered}$ | $\begin{gathered} -.024 \\ (.006) \end{gathered}$ | $\begin{gathered} -.025 \\ (.007) \end{gathered}$ |
| Lot size (1000s) | $\begin{aligned} & .003 \\ & (.0003) \end{aligned}$ | $\begin{aligned} & .005 \\ & (.0005) \end{aligned}$ | $\begin{aligned} & .005 \\ & (.0005) \end{aligned}$ | $\begin{aligned} & .005 \\ & (.0007) \end{aligned}$ | $\begin{gathered} .004 \\ (.0006) \end{gathered}$ |
| Internal square footage (1000s) | .207 (.007) | $\begin{aligned} & .193 \\ & (.01) \end{aligned}$ | .191 (.01) | .195 (.02) | .191 (.012) |
| Age of building | $\begin{gathered} -.002 \\ (.0003) \end{gathered}$ | $\begin{aligned} & -.002 \\ & (.0002) \end{aligned}$ | $\begin{aligned} & -.003 \\ & (.0005) \end{aligned}$ | $\begin{aligned} & -.003 \\ & (.0006) \end{aligned}$ | $\begin{aligned} & -.002 \\ & (.0004) \end{aligned}$ |
| Age squared | $\begin{gathered} .000003 \\ (.000001) \end{gathered}$ | $\begin{aligned} & .000003 \\ & (.0000006) \end{aligned}$ | $\begin{aligned} & .00001 \\ & (.000002) \end{aligned}$ | $\begin{gathered} .000009 \\ (.000003) \end{gathered}$ | $\begin{gathered} .000005 \\ (.000002) \end{gathered}$ |
| Boundary fixed effects | NO | YES | YES | YES | NO |
| Census variables | Yes | No | No | No | Yes |
| N | 22,679 | 10,657 | 6,824 | 4,594 | 4,589 |
| Number of boundaries | N/A | 175 | 174 | 172 | N/A |
| Adjusted $R^{2}$ | 0.6417 | 0.6745 | 0.6719 | 0.6784 | . 6564 |

Differences in Means ${ }^{\text {a }}$

| Distance from boundary: | Full sample |  | 0.35 mile |  | 0.20 mile |  | 0.15 mile |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Difference in means | $T$-statistic | Ratio of 0.35 to full sample ${ }^{\text {d }}$ | $T$-statistic | Ratio of 0.20 to full sample ${ }^{\text {d }}$ | $T$-statistic | Ratio of 0.15 <br> to full sample ${ }^{\text {d }}$ | $T$-statistic |
| $\ln$ (house price) | . 045 | 3.82 | 0.85 | 3.32 | 0.85 | 3.17 | 0.93 | 3.17 |
| Test score (sum of reading and math) | 1.0 | 32.90 | 1.03 | 27.28 | 1.06 | 24.44 | 1.06 | 22.57 |
| House characteristics |  |  |  |  |  |  |  |  |
| Bedrooms | 0.02 | 1.68 | 0.90 | 0.91 | -0.35 | -0.30 | 0.25 | 0.18 |
| Bathrooms | 0.03 | 2.98 | 0.23 | 0.52 | -0.02 | -0.05 | -0.07 | -0.12 |
| Lot size | 2011 | 11.39 | 0.22 | 2.14 | 0.24 | 1.95 | 0.12 | 0.83 |
| Internal square footage | 31 | 2.93 | 0.61 | 1.32 | 0.61 | 1.07 | 0.84 | 1.17 |
| Age of building | -3.13 | -6.92 | 0.75 | -3.71 | 0.94 | -3.76 | 1.09 | -3.52 |
| Neighborhood characteristics ${ }^{\text {c }}$ |  |  |  |  |  |  |  |  |
| Percent Hispanic | -. 0008 | -0.79 | 2.50 | -1.35 | 2.50 | -1.21 | 2.50 | -1.26 |
| Percent non-Hispanic black | -. 0007 | -1.50 | 0.43 | -0.54 | 0.00 | -0.07 | -0.14 | 0.16 |
| Percent 0-9 years old | . 005 | 3.30 | 0.16 | 0.63 | -0.08 | -0.31 | -0.30 | -1.21 |
| Percent 65+ years old | -. 01 | -2.04 | 0.40 | -0.72 | 0.67 | -1.28 | 0.60 | -0.95 |
| Percent female-headed households with children | -. 001 | -3.67 | 1.00 | -3.17 | 1.20 | -2.53 | 1.00 | -2.38 |
| Percent with bachelor's degree | . 002 | 1.06 | 0.75 | 0.64 | 1.00 | 0.74 | 0.75 | 0.67 |
| Percent with graduate degree | . 008 | 3.32 | 0.88 | 2.77 | 0.88 | 3.02 | 0.88 | 3.31 |
| Percent with less than high school diploma | -. 005 | -2.19 | 1.20 | -2.02 | 0.80 | -1.57 | 0.34 | -0.64 |
| Median household income | 2,135 | 2.87 | 0.60 | 1.90 | 0.65 | 2.11 | 0.52 | 1.61 |

TABLE IV
Magnitude of Results ${ }^{\text {a }}$

|  | (1) <br> Basic hedonic regression ${ }^{\text {d }}$ | $\begin{gathered} (2) \\ 0.35 \text { sample } \\ \text { boundary } \\ \text { fixed effects } \end{gathered}$ | (3) <br> 0.20 sample boundary fixed effects | (4) <br> 0.15 sample boundary fixed effects |
| :---: | :---: | :---: | :---: | :---: |
| Coefficient on elementary school test score ${ }^{\text {b }}$ | $\begin{gathered} .035 \\ (.004) \end{gathered}$ | $\begin{gathered} .016 \\ (.007) \end{gathered}$ | $\begin{gathered} .013 \\ (.0065) \end{gathered}$ | $\begin{gathered} .015 \\ (.007) \end{gathered}$ |
| Magnitude of effect (percent change in house price as a result of a $5 \%$ change in test scores) ${ }^{\text {c }}$ | 4.9\% | 2.3\% | 1.8\% | 2.1\% |
| \$ Value (at mean tax-adjusted house price of $\$ 188,000$ in \$1993) | \$9212 | \$4324 | \$3384 | \$3948 |
| \$ Value (at median tax-adjusted house price of $\$ 158,000$ in \$1993) | \$7742 | \$3634 | \$2844 | \$3318 |

a. The results presented here are based on estimates from Table II, columns (1)-(4).
b. Test scores are measured at the elementary school level and represent the sum of the reading and math scores from the fourth grade MEAP test averaged over three years (1988, 1990, and 1992). Source: Massachusetts Department of Education.
c. Approximately a one-standard-deviation change in the average test scores at the mean.
d. Regression includes house characteristics, school characteristics measured at the school district level, and neighborhood characteristics measured at the census block group level. See Table II, column (1), and Appendix 1 for more complete results.

## Does Air Quality Matter? Evidence from the Housing Market

Chay and Greenstone, JPE, 2005.
The goal of this paper is to look at the willingness to pay for clean air

Using their notation

$$
y_{c 80}=X_{c 80}^{\prime} \beta+\theta T_{c 80}+\varepsilon_{c 80}
$$

where

- $y_{c 80}$ is $\log$ of median property value in county $c$ in 1980
- $T_{c 80}$ is the geometric mean of total suspended particulates (TSP)

They focus on the first differenced version of the model

$$
y_{c 80}-y_{c 70}=\left(X_{c 80}-X_{c 70}\right)^{\prime} \beta+\theta\left(T_{c 80}-T_{c 70}\right)+\varepsilon_{c 80}-\varepsilon_{c 70}
$$

They solve the identification problem by making use of the Clean Air Act Amendments of 1970

A county violates federal standards if:

- Annual geometric mean of TSP exceeds $75 \mathrm{ug} / \mathrm{m}$
- Second highest daily measure exceeds 260 ug/m

If you fail the test (non-attainment) the county needs to derive a plan to clean something else

They use failing the test as an instrument for ( $\left.T_{c 80}-T_{c 70}\right)$.

You can see that those that failed had much larger declines


You can also see the discontinuity in pollution and housing prices
(note that there are nonattainers to the left of the line because of the second rule)


Fig. 4.-1970-80 change in mean TSPs by 1975 nonattainment status and the geometric mean of TSPs in 1974.
_- Attainment in 1975


Fig. 5.-1970-80 change in log housing values by 1975 nonattainment status and the geometric mean of TSPs in 1974.

TABLE 2
Differences in Sample Means between Groups of Counties, Defined by TSPs Levels, Changes, or Nonattainment Status

|  | Cross <br> Section 1970 <br> (1) | First <br> Difference <br> 1980-1970 <br> (2) | TSPs Nonattainment |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\begin{aligned} & \text { In 1970, } \\ & \text { 1971, or } \\ & 1972 \\ & (3) \end{aligned}$ | In 1975 or 1976 <br> (4) | In 1975 Regression Discontinuity Sample <br> (5) | In 1975 Bad Day Sample <br> (6) |
| Total counties (nonattainment) | 988 | 988 | $\begin{gathered} 988 \\ (380) \end{gathered}$ | $\begin{gathered} 988 \\ (280) \end{gathered}$ | $\begin{aligned} & 475 \\ & (123) \end{aligned}$ | $\begin{aligned} & 419 \\ & (67) \end{aligned}$ |
| Housing value | $\begin{aligned} & 1,092 \\ & (918) \end{aligned}$ | $\begin{gathered} -3,237 * * \\ (713) \end{gathered}$ | $\begin{array}{r} -517 \\ (726) \end{array}$ | $\begin{gathered} 2,609^{* *} \\ (806) \end{gathered}$ | $\begin{gathered} 2,007 \\ (1,193) \end{gathered}$ | $\begin{gathered} 2,503 \\ (1,585) \end{gathered}$ |
| Mean TSPs | $\begin{aligned} & 39.2^{* *} \\ & (1.2) \end{aligned}$ | $\begin{gathered} -30.9^{* *} \\ (1.0) \end{gathered}$ | $\begin{gathered} -19.6^{* *} \\ (1.4) \end{gathered}$ | $\begin{gathered} -10.0^{* *} \\ (1.8) \end{gathered}$ | $\begin{gathered} -12.3^{* *} \\ (2.4) \end{gathered}$ | $\begin{gathered} -4.8 \\ (2.9) \end{gathered}$ |
| Economic condition variables: Income per capita (1982-84 dollars) | $\begin{aligned} & 377.7^{* *} \\ & (94.7) \end{aligned}$ | $\begin{gathered} -159.9^{* *} \\ (40.7) \end{gathered}$ | $\begin{gathered} -81.6^{*} \\ (41.2) \end{gathered}$ | $\begin{gathered} 48.6 \\ (46.4) \end{gathered}$ | $\begin{gathered} 47.2 \\ (65.1) \end{gathered}$ | $\begin{gathered} -37.2 \\ (94.1) \end{gathered}$ |
| Total population (\% change) | $\begin{gathered} 142,016 * * \\ (24,279) \end{gathered}$ | $\begin{gathered} -.058^{* *} \\ (.013) \end{gathered}$ | $\begin{gathered} -.046^{* *} \\ (.013) \end{gathered}$ | $\begin{gathered} -.001 \\ (.017) \end{gathered}$ | $\begin{gathered} .005 \\ (.028) \end{gathered}$ | $\begin{gathered} .015 \\ (.030) \end{gathered}$ |
| Unemployment rate ( $\times 100$ ) | $\begin{gathered} -.144 \\ (.120) \end{gathered}$ | $\begin{gathered} .519 * * \\ (.129) \end{gathered}$ | $\begin{gathered} .200 \\ (.132) \end{gathered}$ | $\begin{gathered} .043 \\ (.152) \end{gathered}$ | $\begin{gathered} .305 \\ (.215) \end{gathered}$ | $\begin{array}{r} -.032 \\ (.274) \end{array}$ |
| \% employment in manufacturing $(\times 10)$ | $\begin{gathered} .098 \\ (.083) \end{gathered}$ | $\begin{gathered} -.119 * * \\ (.026) \end{gathered}$ | $\begin{gathered} -.081^{* *} \\ (.026) \end{gathered}$ | $\begin{gathered} -.005 \\ (.028) \end{gathered}$ | $\begin{array}{r} -.057 \\ (.042) \end{array}$ | $\begin{array}{r} -.066 \\ (.051) \end{array}$ |

TABLE 3
Cross-Sectional and First-Difference Estimates of the Effect of TSPs Pollution on Log Housing Values

|  | (1) | (2) | (3) | (4) |
| :---: | :---: | :---: | :---: | :---: |
| Mean TSPs (1/100) | A. 1970 Cross Section |  |  |  |
|  | . 032 | $\begin{aligned} & -.062 \\ & (.018) \end{aligned}$ | $\begin{aligned} & -.040 \\ & (.017) \end{aligned}$ | $\begin{aligned} & -.024 \\ & (.017) \end{aligned}$ |
|  | (.038) |  |  |  |
| $R^{2}$ <br> Sample size | . 00 | $\begin{aligned} & .79 \\ & 987 \end{aligned}$ | . 84 | $\begin{array}{r} .85 \\ 987 \end{array}$ |
|  | 988 |  | 987 |  |
|  | B. 1980 Cross Section |  |  |  |
| Mean TSPs (1/100) | . 093 | $\begin{gathered} .096 \\ (.031) \end{gathered}$ | $\begin{gathered} .076 \\ (.030) \end{gathered}$ | $\begin{gathered} .027 \\ (.028) \end{gathered}$ |
|  | (.066) |  |  |  |
| $R^{2}$ <br> Sample size | . 00 | $\begin{aligned} & .82 \\ & 984 \end{aligned}$ | $\begin{gathered} .89 \\ 984 \end{gathered}$ | $\begin{array}{r} .89 \\ 984 \end{array}$ |
|  | 988 |  |  |  |
| Mean TSPs (1/100) | C. 1970-80 (First Differences) |  |  |  |
|  | . 102 | . 024 | . 004 | -. 006 |
|  | (.032) | (.020) | (.016) | (.014) |
| $R^{2}$ | . 02 | . 55 | . 65 | . 73 |
| Sample size | 988 | 983 | 983 | 983 |
| County Data Book covariates | no | yes | yes | yes |
| Flexible form of county covariates | no | no | yes | yes |
| Region fixed effects | no | no | no | yes |

## TABLE 4

Estimates of the Impact of Mid-Decade TSPs Nonattainment on 1970-80 Changes in TSPs Pollution and Log Housing Values

|  | $(1)$ | $(2)$ | $(3)$ | $(4)$ |
| :--- | :---: | :---: | :---: | :---: |
|  |  |  |  |  |
|  | A. Mean TSPs Changes |  |  |  |
| TSPs nonattainment in 1975 | -9.96 | -10.41 | -9.57 | -9.40 |
| or 1976 | $(1.78)$ | $(1.90)$ | $(1.94)$ | $(2.02)$ |
| $F$-statistic TSPs | 31.3 | 29.9 | 24.4 | 21.5 |
| nonattainment* | $(1)$ | $(1)$ | $(1)$ | $(1)$ |
| $R^{2}$ | .04 | .10 | .19 | .20 |
|  | B. Log Housing Changes |  |  |  |
|  |  | .036 | .022 | .026 |
| TSPs nonattainment in 1975 | $(.012)$ | $(.009)$ | $(.008)$ | $(.008$ |
| or 1976 | 8.5 | 6.2 | 9.3 | 6.4 |
| $F$-statistic TSPs | $(1)$ | $(1)$ | $(1)$ | $(1)$ |
| nonattainment* | .01 | .56 | .66 | .73 |
| $R^{2}$ | $n o$ | yes | yes | yes |
| County Data Book covariates |  |  |  |  |
| Flexible form of county | no | no | yes | yes |
| covariates | no | no | no | yes |
| Region fixed effects | 988 | 983 | 983 | 983 |
| Sample size |  |  |  |  |

TABLE 5
Instrumental Variables Estimates of the Effect of 1970-80 Changes in TSPs Pollution on Changes in Log Housing Values

|  | (1) | (2) | (3) | (4) |
| :---: | :---: | :---: | :---: | :---: |
| Mean TSPs (1/100) | A. TSPs Nonattainment in 1975 or 1976 |  |  |  |
|  | $-.362$ | -. 213 | -. 266 | -. 202 |
|  | (.152) | (.096) | (.104) | (.090) |
| Sample size | 988 | 983 | 983 | 983 |
|  | B. TSPs Nonattainment in 1975 |  |  |  |
| Mean TSPs (1/100) | -. 350 | -. 204 | -. 228 | -. 129 |
|  | (.150) | (.099) | (.102) | (.084) |
| Sample size | 975 | 968 | 968 | 968 |
|  | C. TSPs Nonattainment in 1970, 1971, or 1972 |  |  |  |
| Mean TSPs (1/100) | . 072 | -. 032 | -. 050 | -. 073 |
|  | (.058) | (.042) | (.041) | (.035) |
| Sample size | 988 | 983 | 983 | 983 |
| County Data Book covariates | no | yes | yes | yes |
| Flexible form of county <br> covariates no no yes yes |  |  |  |  |
| Region fixed effects | no | no | no | yes |







[^0]:    Variable definitions are as follows: Class size $=$ number of students in class in the spring, Enrollment $=$

[^1]:    The unit of observation is the average sccre in the class. Standard errors are reported in parentheses. Standard errors were corrected for within-school correlation between classes. All estimates use $f_{c x}$ as an instrument for class size.

