

Problem Set 1
Econometrics 718
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Due: Wed. Feb. 21

Problem 1. Take any data set you would like and with any software you would like think about the exactly identified IV problem. I would like you to produce the IV estimate in three different ways and show they are numerically equivalent (I don't care whether the instrument is really uncorrelated with the residual):

- a) IV, that is $(Z'X)^{-1}Z'Y$ (you can use `ivregress` with the `gmm` option in `stata`)
- b) Two staged least squares. That is first run the treatment variable on the instrument and the X's, form the predicted value, then run a regression of the outcome on the predicted value and the other X's.
- c) Ratio of reduced form coefficients. Run the two reduced forms and take the ratio of the coefficients on the Z.

Problem 2. Verify the measurement error result. That is I want you to use your statistical package to construct

- T_i to have whatever distribution you want (a uniform might be easy)
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$$Y_i = \beta_0 + \beta_1 T_i + u_i$$

where u_i is $N(0, \sigma_u^2)$. You can choose these parameters to be anything you want.

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$$\tau_{1i} = T_i + \xi_i$$

where ξ_i is $N(0, \sigma_\xi^2)$

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$$\tau_{2i} = T_i + \eta_i$$

where η_i is $N(0, \sigma_\eta^2)$

Show that

- a) If you run a regression of Y_i on T_i you get something close to β_1
- b) If you run a regression of Y_i on τ_{1i} you get something close to

$$\beta_1 \frac{\text{Var}(T_i)}{\text{Var}(T_i) + \sigma_\xi^2}$$

- c) Doing IV using τ_{2i} as an instrument for τ_{1i} gives an estimate close to β_1