

Solow Model Equations

(I) Solow with population growth and no technological change.

(population = # of workers)

$$(1) \quad Y = K^\alpha L^{1-\alpha}$$

$$(2) \quad \stackrel{\wedge}{L} = n, \quad S = s \stackrel{\wedge}{Y}, \quad C = (1 - s) \stackrel{\wedge}{Y}$$

$$(3) \quad \Delta K = s \stackrel{\wedge}{Y} - \delta K$$

$$(4) \quad \stackrel{\wedge}{K} = s (\stackrel{\wedge}{Y} / K) - \delta$$

Y = output, K = capital, L = labor

Define new variables :

$$y = Y/L \text{ (output per worker)}, \quad k = K/L \text{ (capital per worker)}$$

$$(5) \quad \Delta k = s y - (\delta + n) k$$

(II) Solow with technological change and population growth

(population = # of workers)

$$(1) \quad Y = K^\alpha (AL)^{1-\alpha}$$

$$(2) \quad \stackrel{\wedge}{L} = n, \quad \stackrel{\wedge}{A} = g, \quad S = s \stackrel{\wedge}{Y}, \quad C = (1 - s) \stackrel{\wedge}{Y}$$

$$(3) \quad \Delta K = s \stackrel{\wedge}{Y} - \delta K$$

Define new variables :

$$\tilde{k} = K / L A \text{ (capital per effective unit of labor)}, \quad \tilde{y} = Y / L A \text{ (output per effective unit of labor)}$$

$$(4) \quad \tilde{\Delta} k = s \tilde{y} - (\delta + n + g) \tilde{k}$$